## Lecture 18:

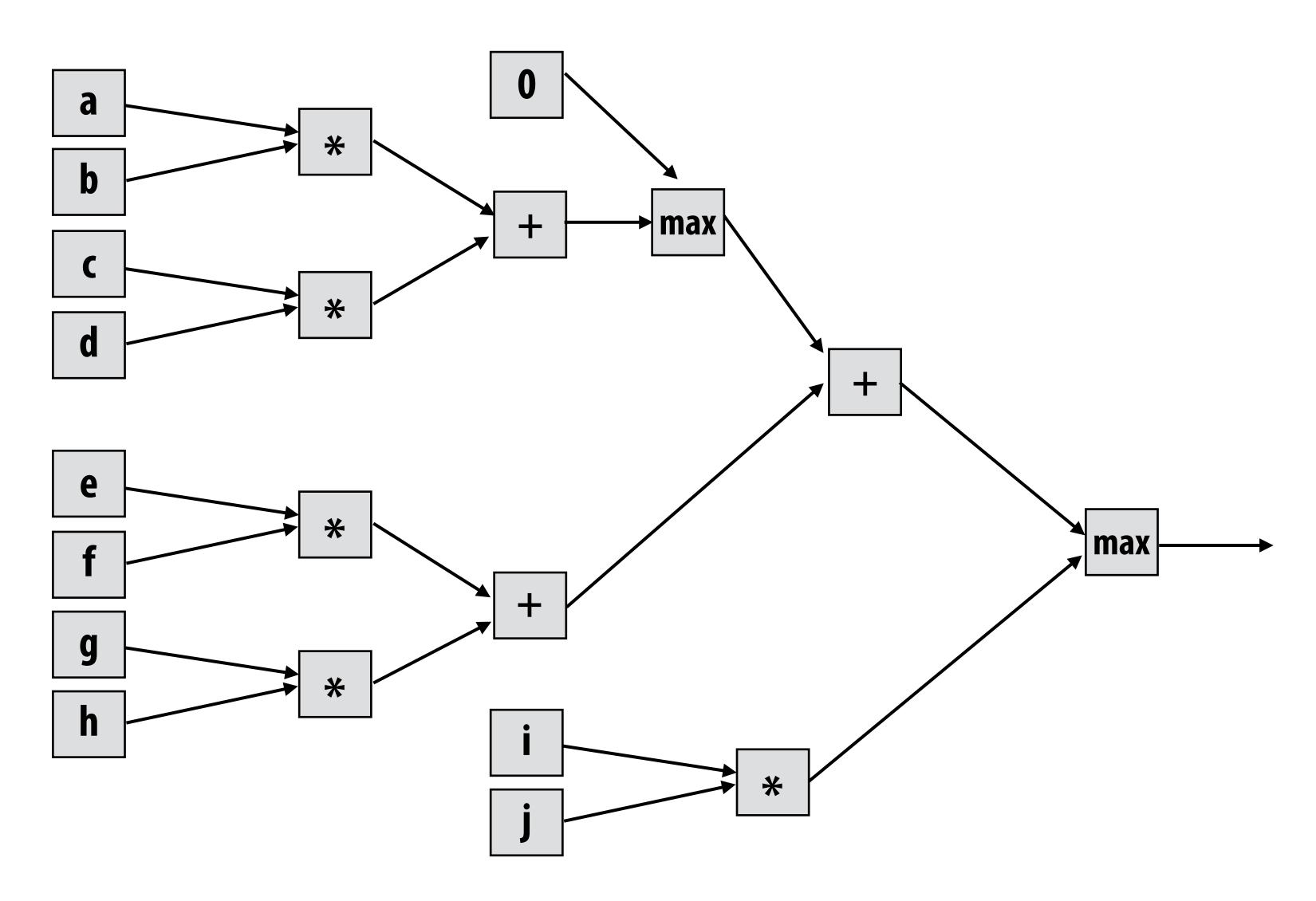
# Efficiently Evaluating DNNs

Parallel Computing
Stanford CS149, Fall 2020

## Today

- We will discuss the workload of <u>evaluating</u> deep neural networks (performing "inference")
  - This lecture will be heavily biased towards concerns of DNNs that process images (to be honest, because that is what your instructor knows best)
  - But, image processing is not the application driving the majority of DNN evaluation in the world right now (its text processing, speech, ads, etc.)

## Consider the following expression

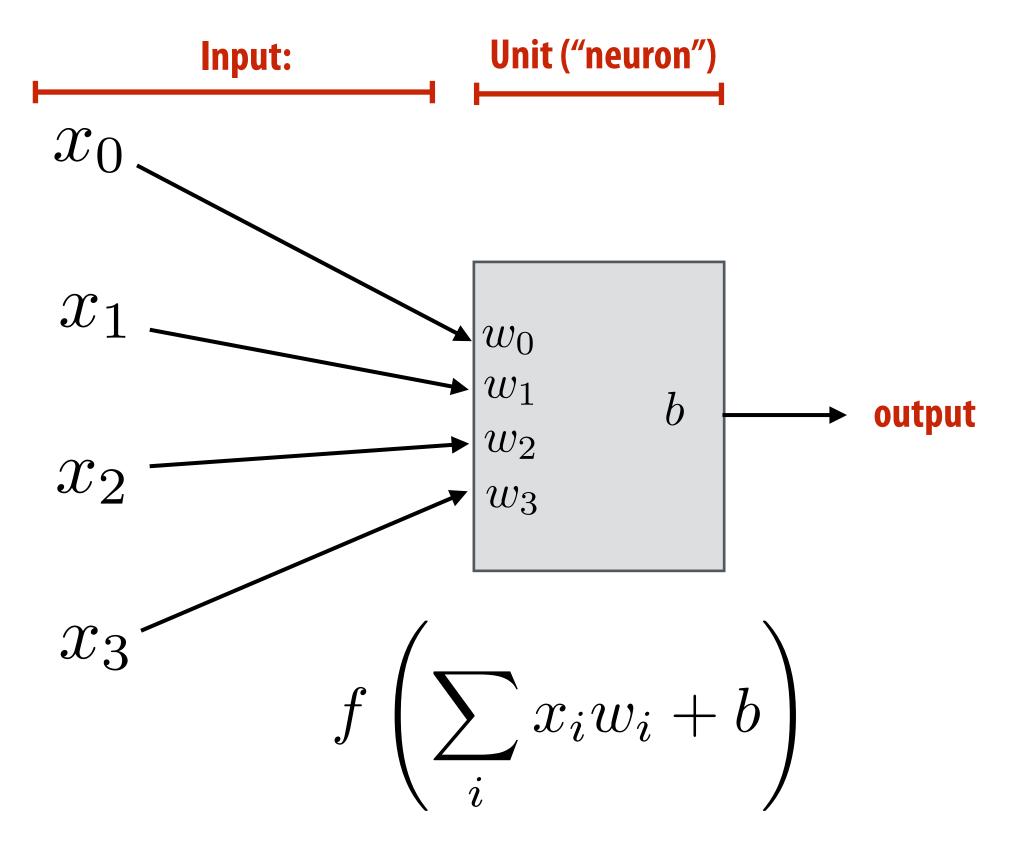


max(max(0, (a\*b) + (c\*d)) + (e\*f) + (g\*h), i\*j)

## What is a deep neural network?

## A basic unit:

Unit with n inputs described by n+1 parameters (weights + bias)

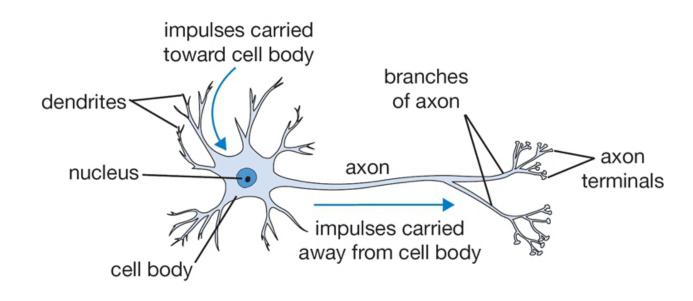


**Example: rectified linear unit (ReLU)** 

$$f(x) = max(0, x)$$

Basic computational interpretation: It is just a circuit!

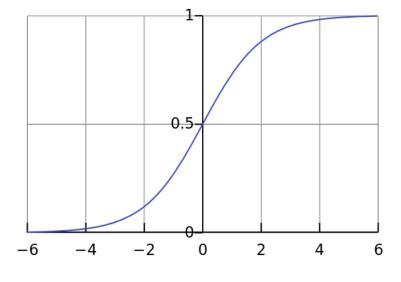
Biological inspiration: unit output corresponds loosely to activation of neuron



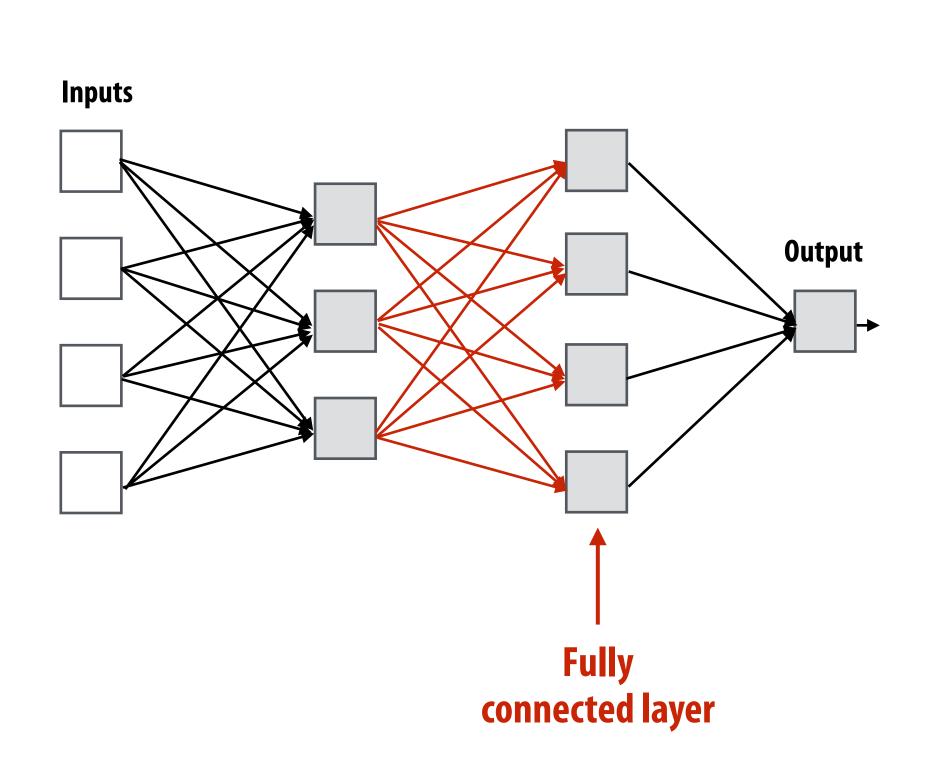
### **Machine learning interpretation:**

binary classifier: interpret output as the probability of one class

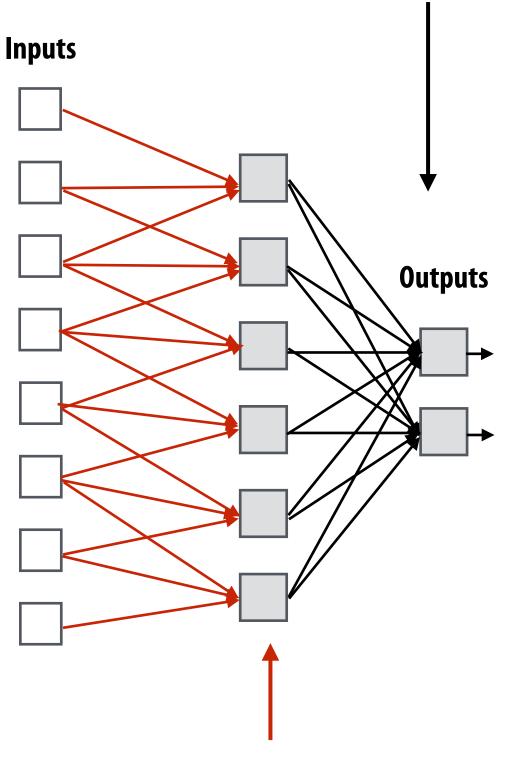
$$f(x) = \frac{1}{1 + e^{-x}}$$



## Deep neural network: topology



## Fully connected layer



Sparsely (locally)
connected layer
(each unit only received inputs
from three input nodes)

## Recall image convolution (3x3 conv)

```
Inputs
int WIDTH = 1024;
                                                                                                                                                                                                          Inputs
int HEIGHT = 1024;
                                                                                                                                                                                                                                                                 Conv
                                                                                                                                                                                                                                                                Layer
float input[(WIDTH+2) * (HEIGHT+2)];
float output[WIDTH * HEIGHT];
float weights[] = \{1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.0/9, 1.
                                                                                       1.0/9, 1.0/9, 1.0/9,
                                                                                       1.0/9, 1.0/9, 1.0/9};
for (int j=0; j<HEIGHT; j++) {</pre>
                                                                                                                                                                                               Convolutional layer: locally connected AND all units in layer
         for (int i=0; i<WIDTH; i++) {
                                                                                                                                                                                               share the same parameters (same weights + same bias):
                  float tmp = 0.f;
                                                                                                                                                                                               (note: network illustration above only shows links for a 1D conv:
                  for (int jj=0; jj<3; jj++)
                                                                                                                                                                                                a.k.a. one iteration of ii loop)
                           for (int ii=0; ii<3; ii++)
                                    tmp += input[(j+jj)*(WIDTH+2) + (i+ii)] * weights[jj*3 + ii];
                  output[j*WIDTH + i] = tmp;
```

# What does convolution using these filter

weights do?

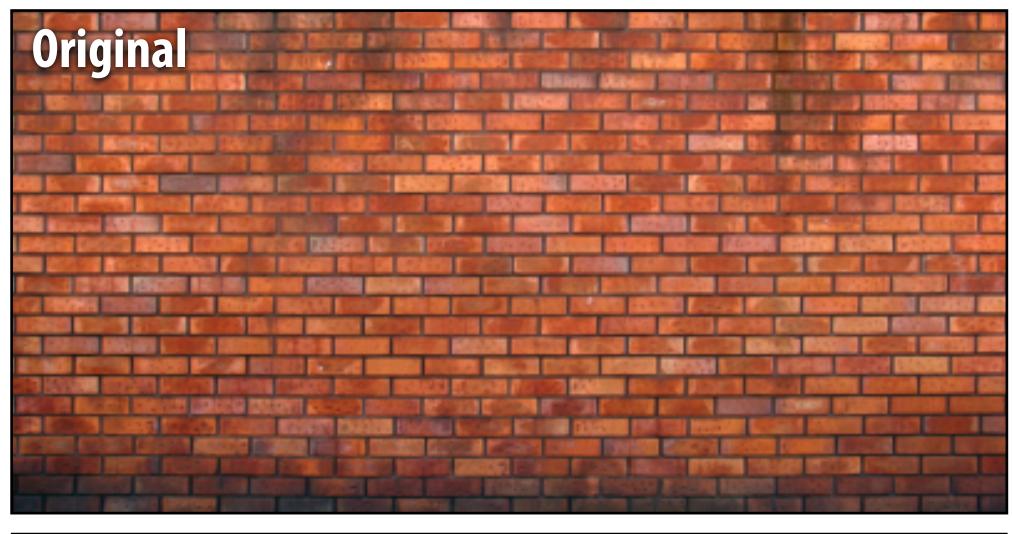
```
      .111
      .111

      .111
      .111

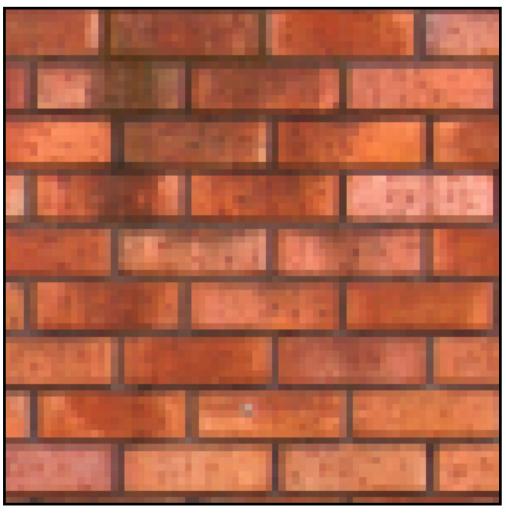
      .111
      .111

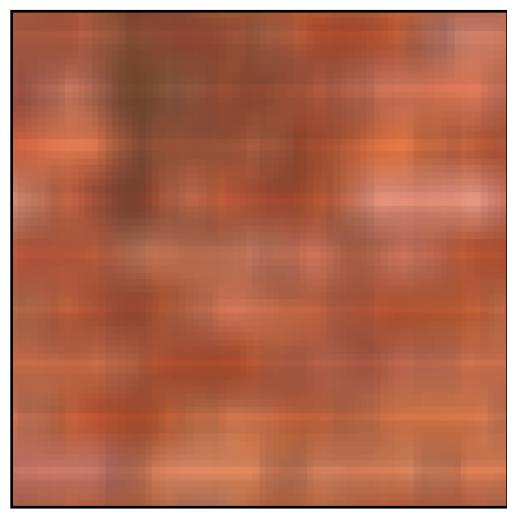
      .111
      .111
```

"Box blur"









## What does convolution with these filters do?

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} \qquad \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

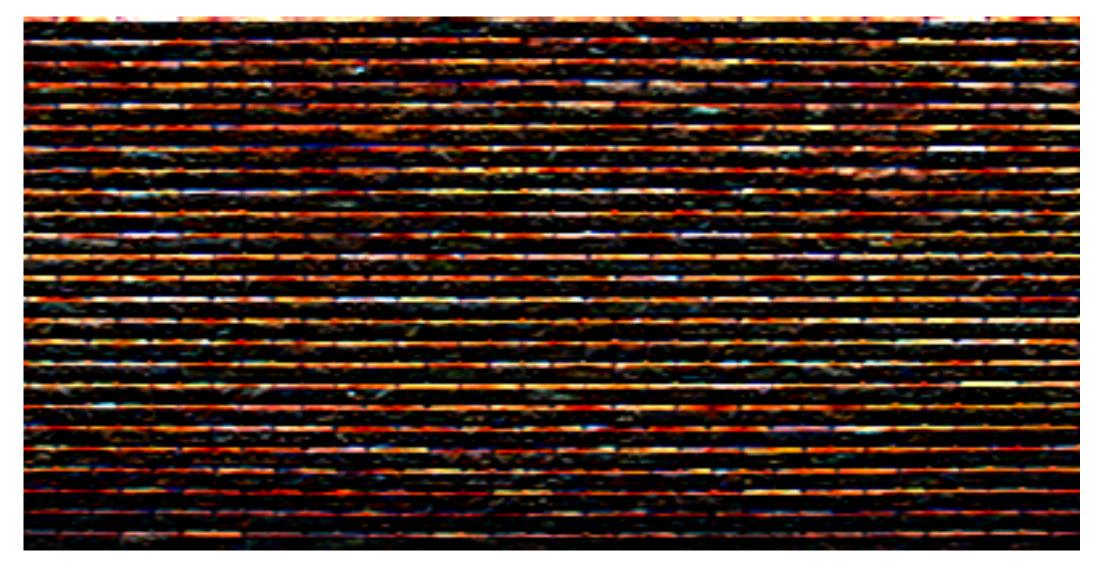
**Extracts horizontal** gradients

**Extracts vertical** gradients

## Gradient detection filters



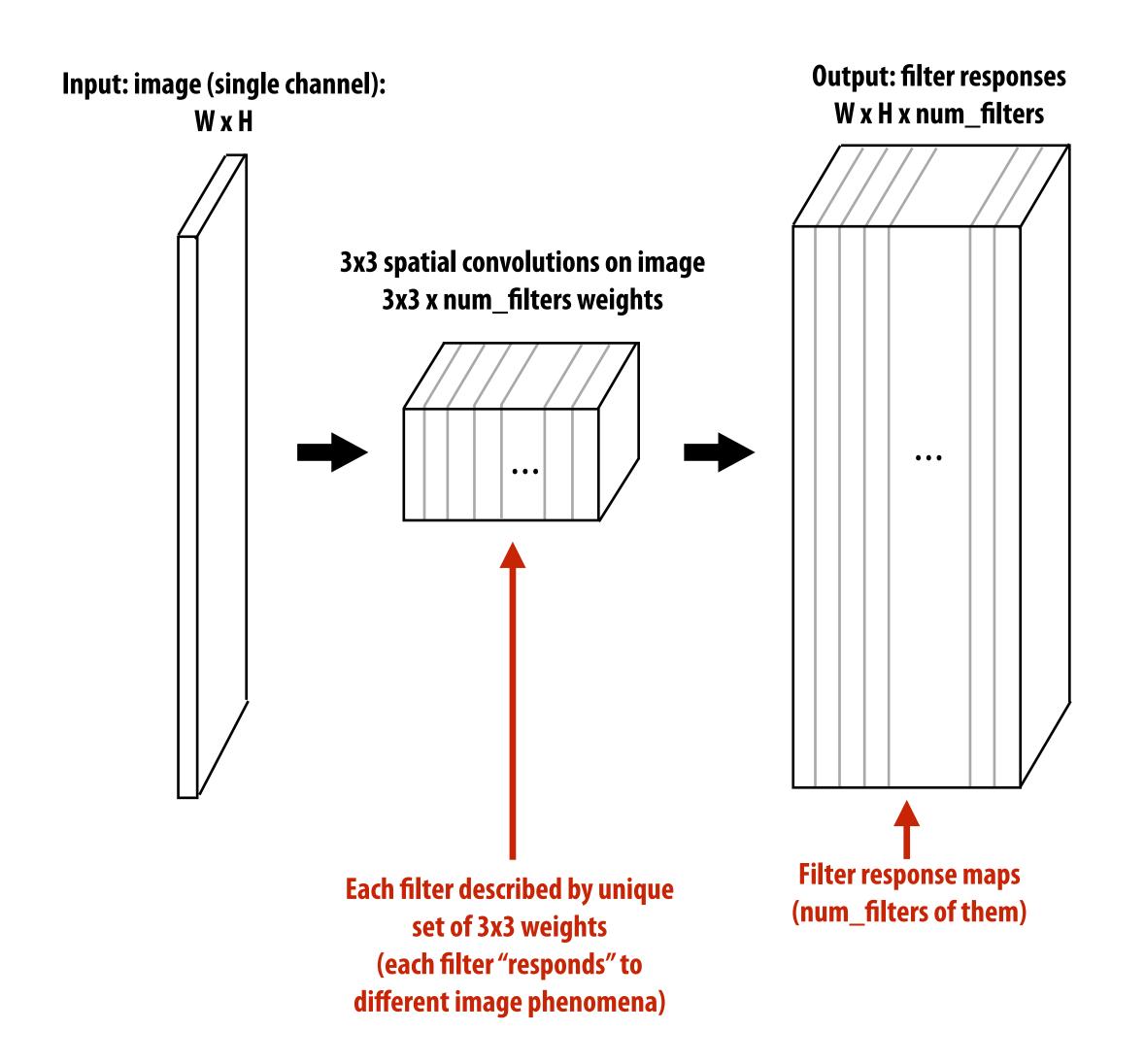
### **Horizontal gradients**



## **Vertical gradients**

Note: you can think of a filter as a "detector" of a pattern, and the magnitude of a pixel in the output image as the "response" of the filter to the region surrounding each pixel in the input image

## Applying many filters to an image at once

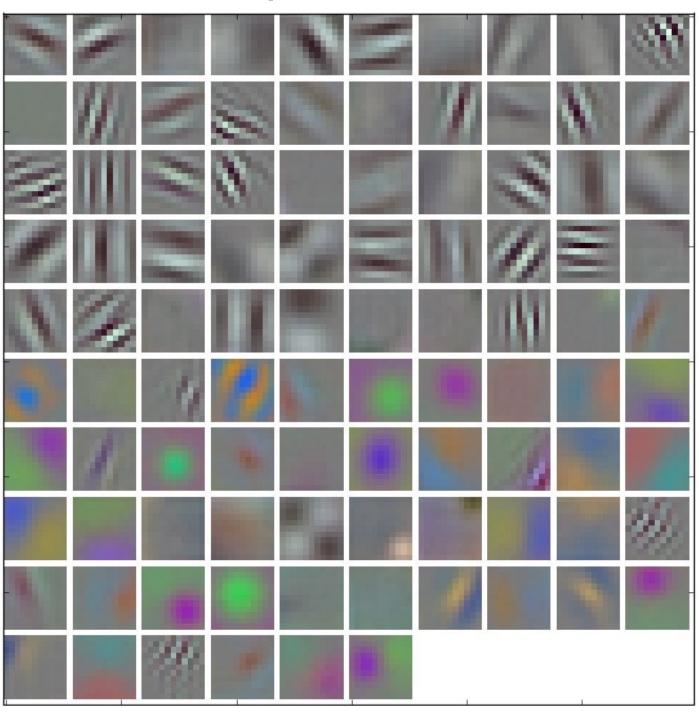


# Applying many filters to an image at once

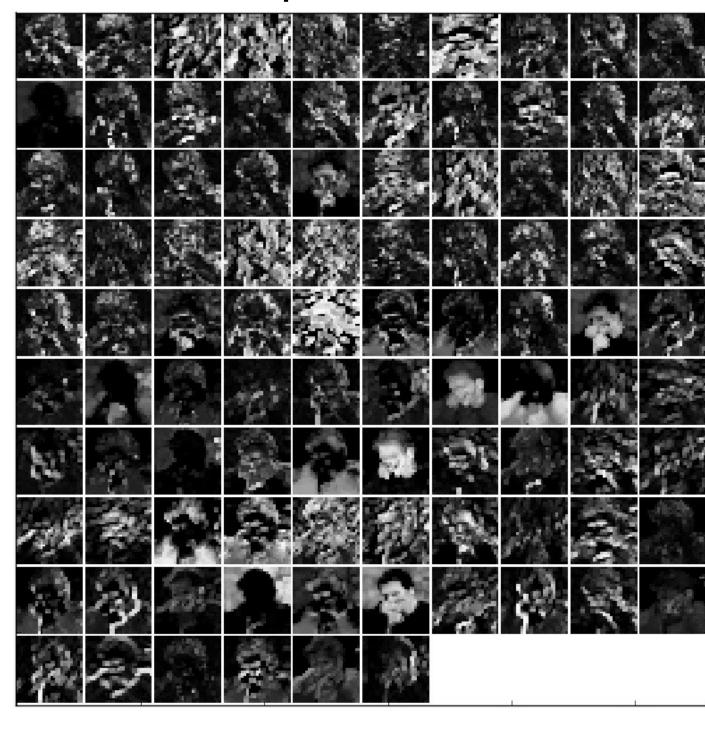
Input RGB image (W x H x 3)



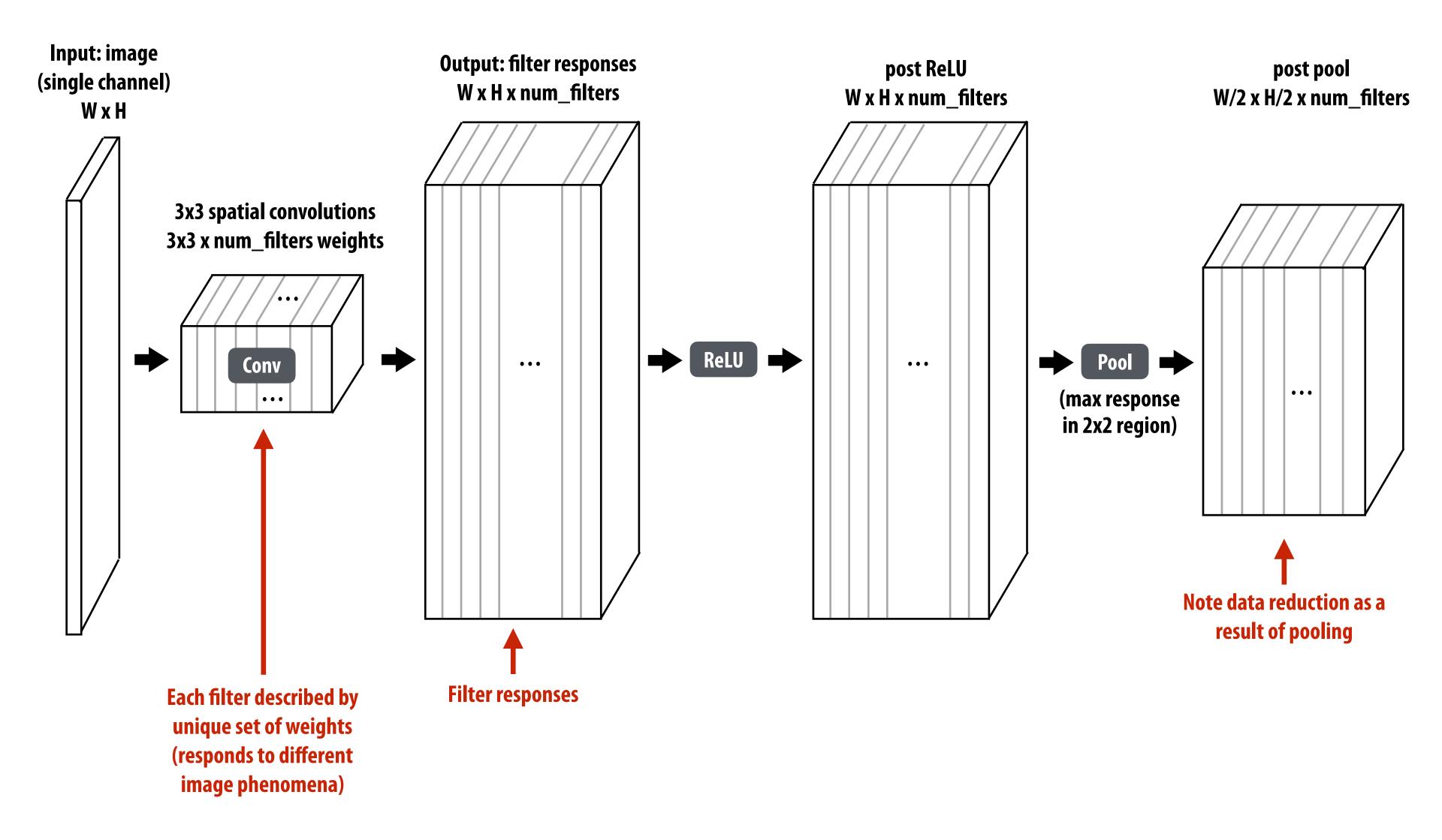
96 11x11x3 filters (operate on RGB)



96 responses (normalized)



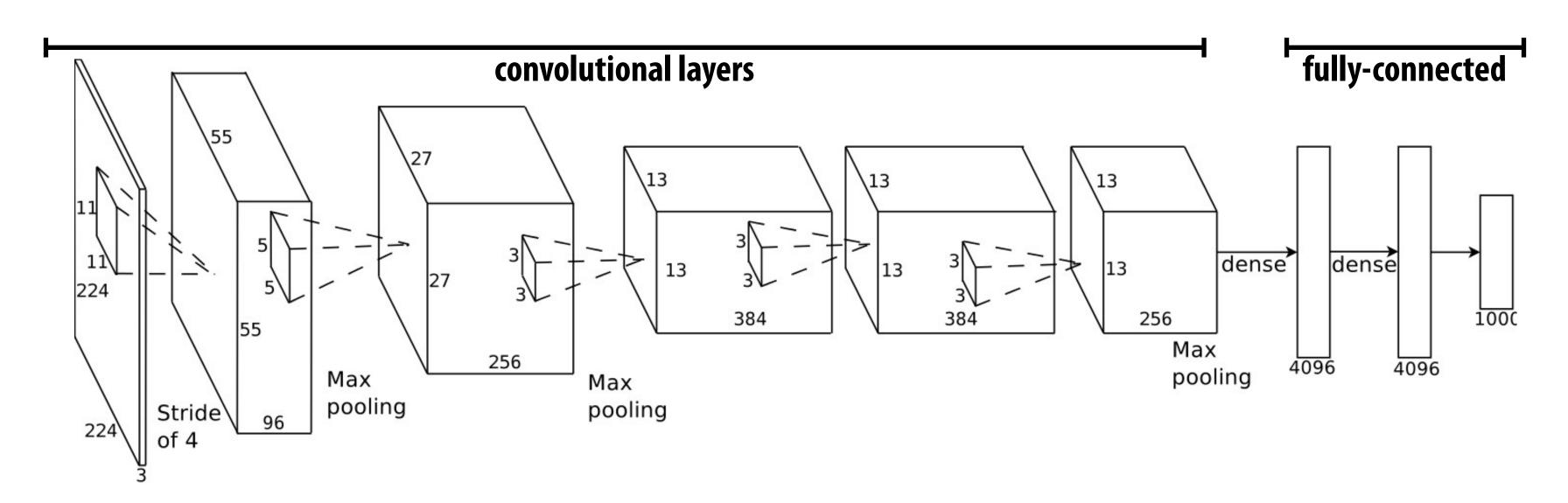
# Adding additional layers



## Example: "AlexNet" object detection network

Sequences of conv + reLU + pool (optional) layers

Example: AlexNet [Krizhevsky12]: 5 convolutional layers + 3 fully connected layers



#### Another example: VGG-16 [Simonyan15]: 13 convolutional layers

conv/reLU: 3x3x128x128

maxpool

input: 224 x 224 RGB conv/reLU: 3x3x128x256 conv/reLU: 3x3x512x512 conv/reLU: 3x3x3x64 conv/reLU: 3x3x256x256 conv/reLU: 3x3x512x512 conv/reLU: 3x3x64x64 conv/reLU: 3x3x256x256 conv/reLU: 3x3x512x512 maxpool maxpool maxpool conv/reLU: 3x3x64x128 conv/reLU: 3x3x256x512 fully-connected 4096

conv/reLU: 3x3x256x512 fully-connected 4096 conv/reLU: 3x3x512x512 fully-connected 4096 conv/reLU: 3x3x512x512 fully-connected 1000

maxpool soft-max

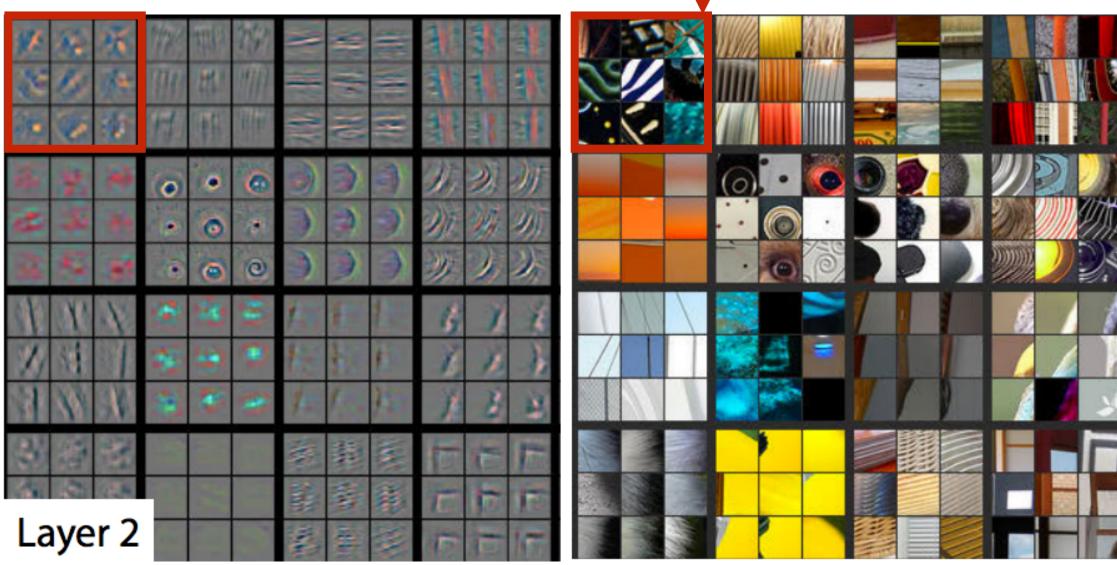
## Why deep?

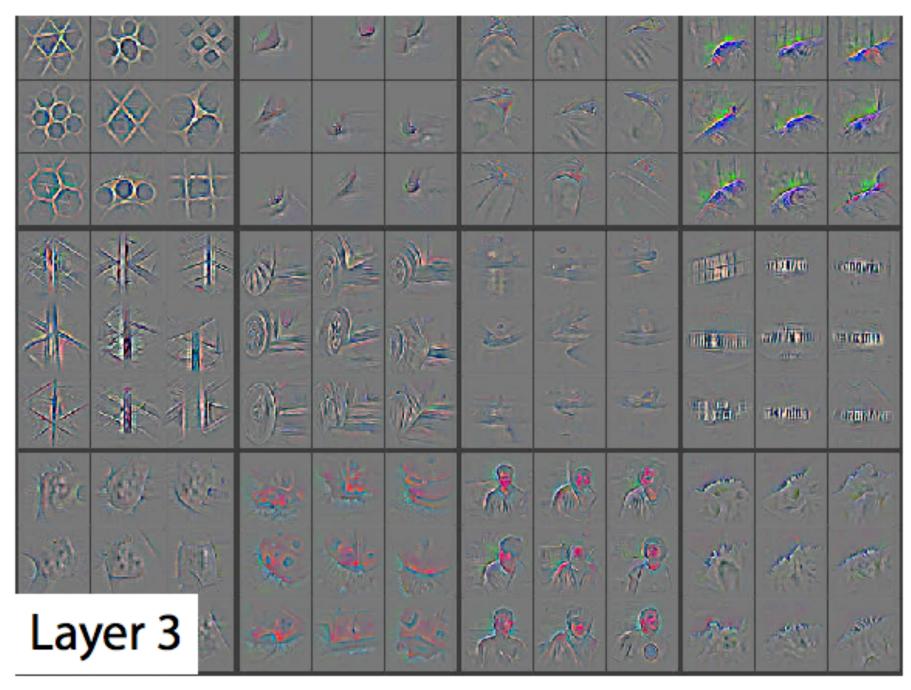


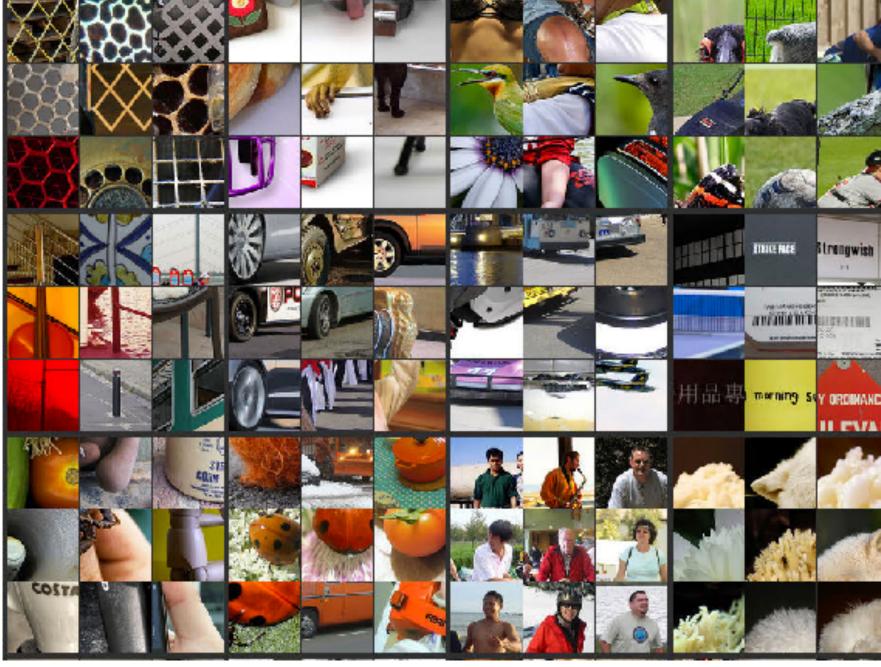
Layer 1



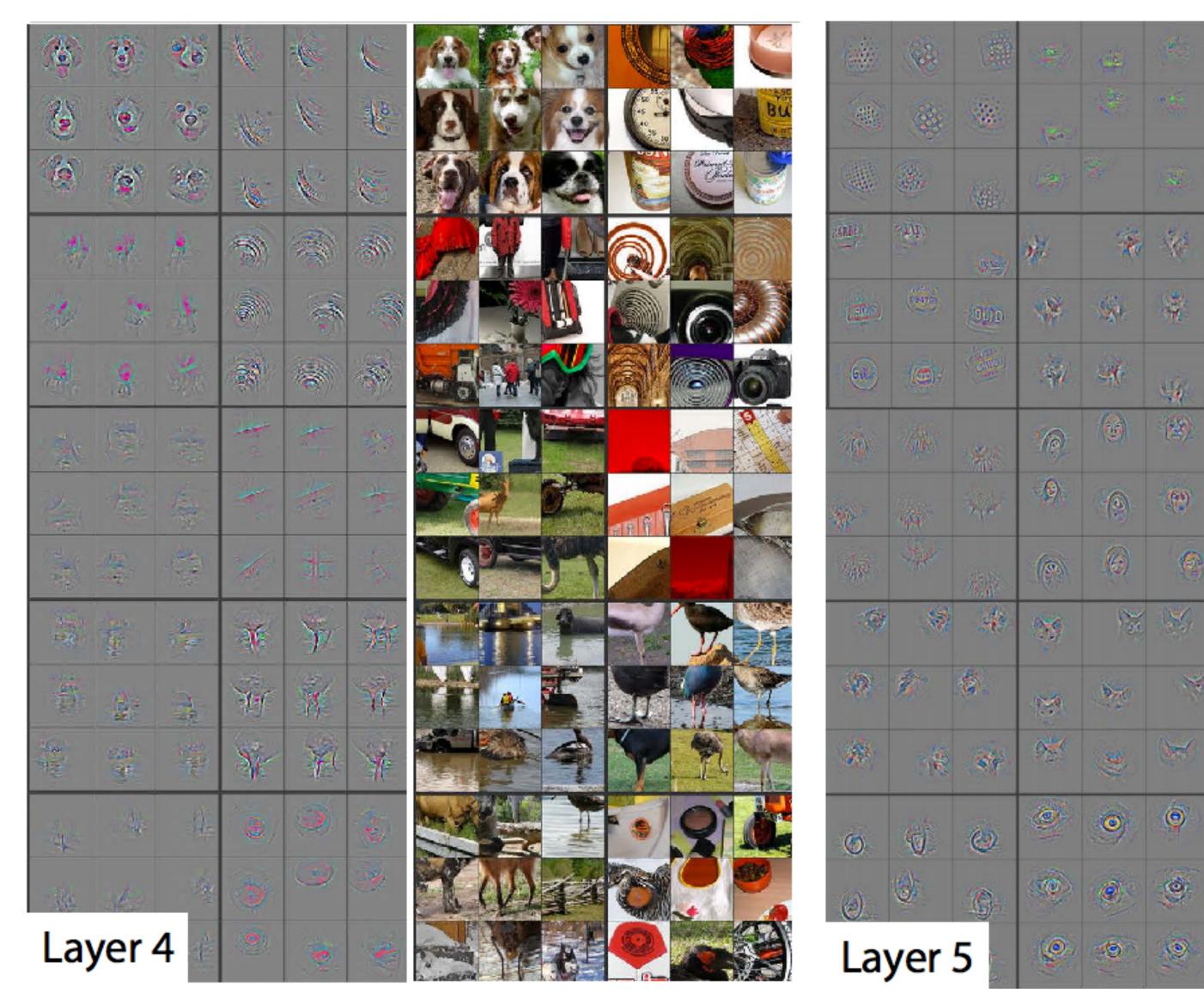








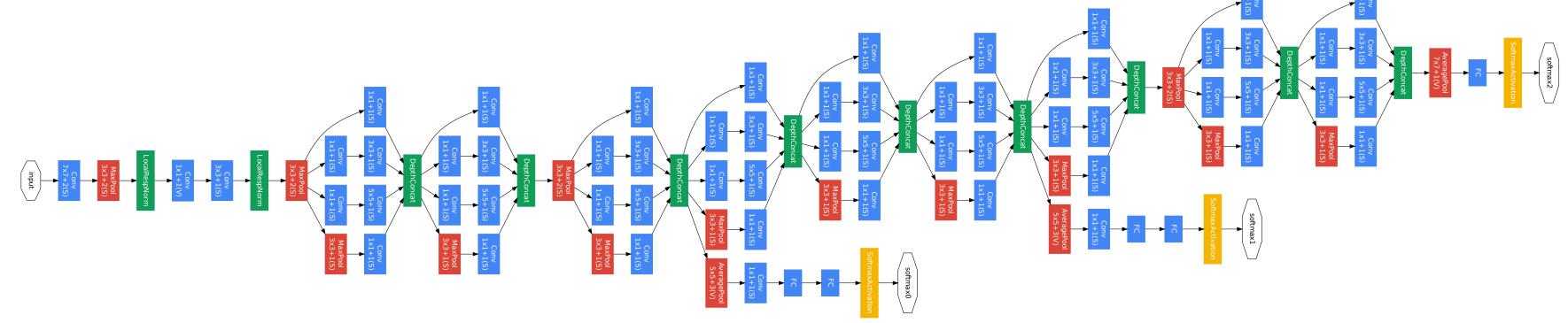
## Why deep?



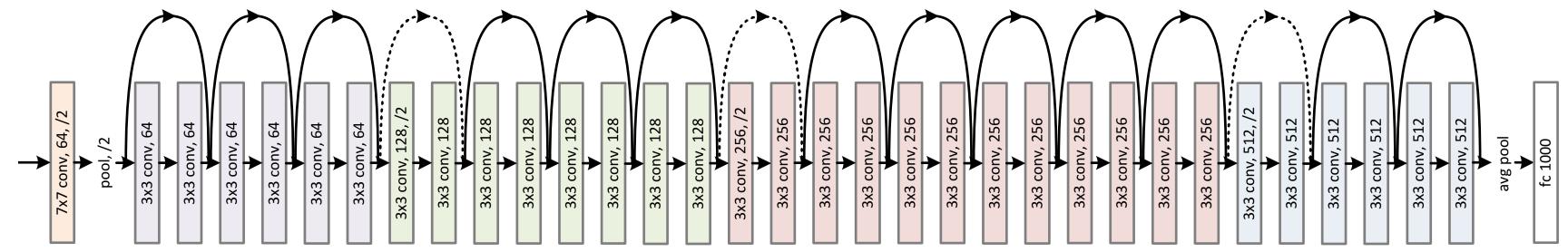


[image credit: Zeiler 14]

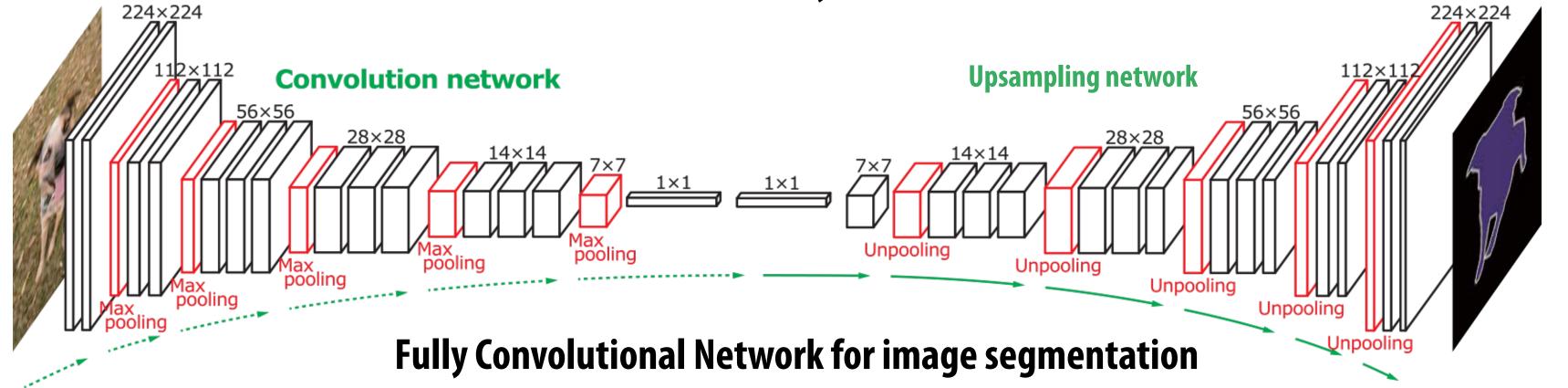
## More recent image understanding networks



Inception (GoogleLeNet)



**ResNet (34 layer version)** 



# Efficiently implementing convolution layers

## Dense matrix multiplication

What is the problem with this implementation?

Low arithmetic intensity (does not exploit temporal locality in access to A and B)

## Blocked dense matrix multiplication

```
float A[M][K];
float B[K][N];
float C[M][N];
   compute C += A * B
#pragma omp parallel for
for (int jblock=0; jblock<M; jblock+=BLOCKSIZE_J)</pre>
  for (int iblock=0; iblock<N; iblock+=BLOCKSIZE_I)</pre>
     for (int kblock=0; kblock<K; kblock+=BLOCKSIZE_K)</pre>
        for (int j=0; j<BLOCKSIZE_J; j++)</pre>
            for (int i=0; i<BLOCKSIZE_I; i++)</pre>
               for (int k=0; k<BLOCKSIZE_K; k++)</pre>
                  C[jblock+j][iblock+i] += A[jblock+j][kblock+k] * B[kblock+k][iblock+i];
```

Idea: compute partial result for block of C while required blocks of A and B remain in cache (Assumes BLOCKSIZE chosen to allow block of A, B, and C to remain resident)

Self check: do you want as big a BLOCKSIZE as possible? Why?

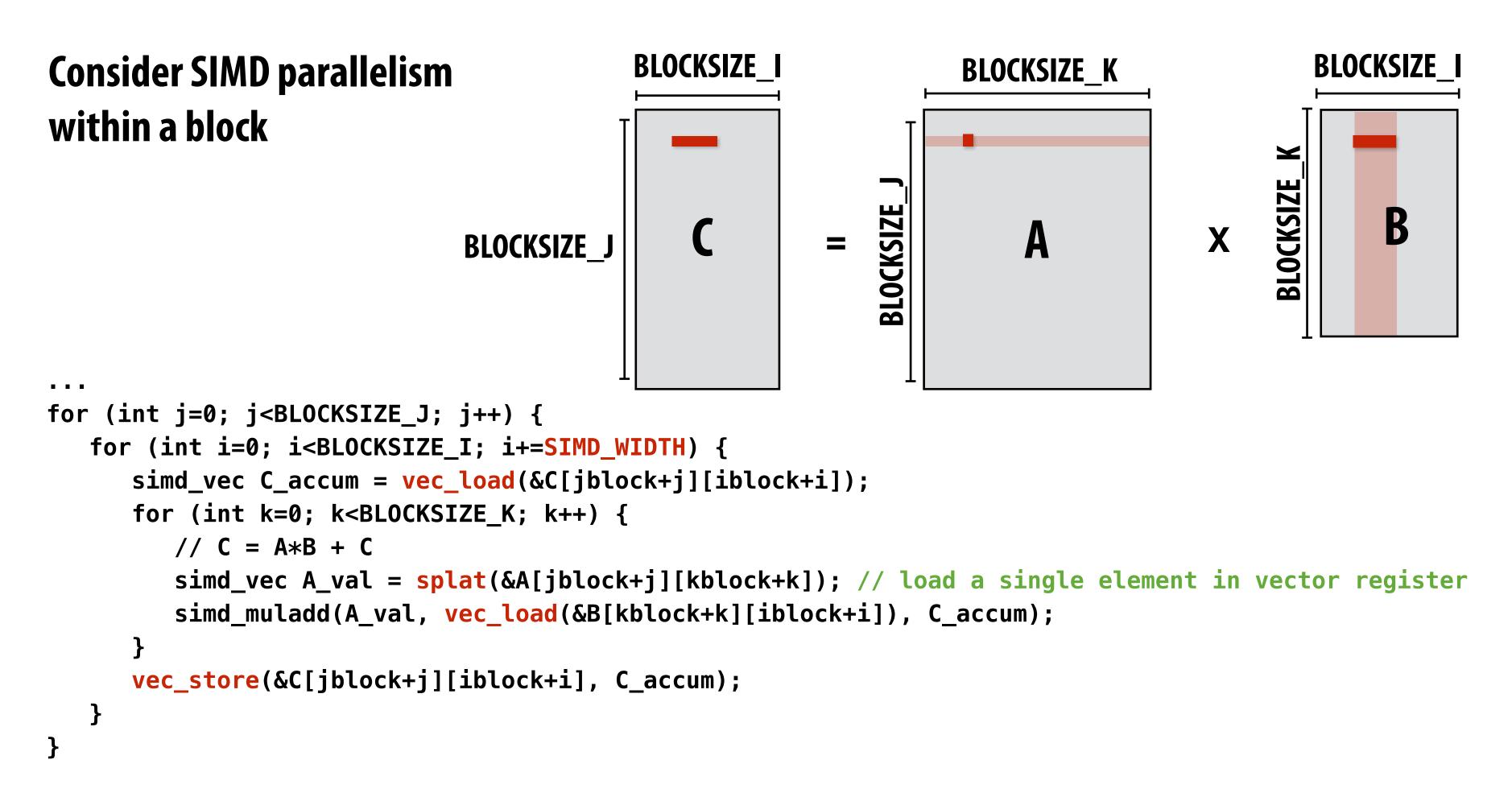
## Hierarchical blocked matrix mult

### **Exploit multiple levels of memory hierarchy**

```
float A[M][K];
float B[K][N];
float C[M][N];
// compute C += A * B
#pragma omp parallel for
for (int jblock2=0; jblock2<M; jblock2+=L2_BLOCKSIZE_J)</pre>
  for (int iblock2=0; iblock2<N; iblock2+=L2_BLOCKSIZE_I)</pre>
     for (int kblock2=0; kblock2<K; kblock2+=L2_BLOCKSIZE_K)</pre>
         for (int jblock1=0; jblock1<L1_BLOCKSIZE_J; jblock1+=L1_BLOCKSIZE_J)</pre>
            for (int iblock1=0; iblock1<L1_BLOCKSIZE_I; iblock1+=L1_BLOCKSIZE_I)</pre>
               for (int kblock1=0; kblock1<L1_BLOCKSIZE_K; kblock1+=L1_BLOCKSIZE_K)</pre>
                    for (int j=0; j<BLOCKSIZE_J; j++)</pre>
                       for (int i=0; i<BLOCKSIZE_I; i++)</pre>
                          for (int k=0; k<BLOCKSIZE_K; k++)</pre>
```

Not shown: final level of "blocking" for register locality...

# Blocked dense matrix multiplication (1)

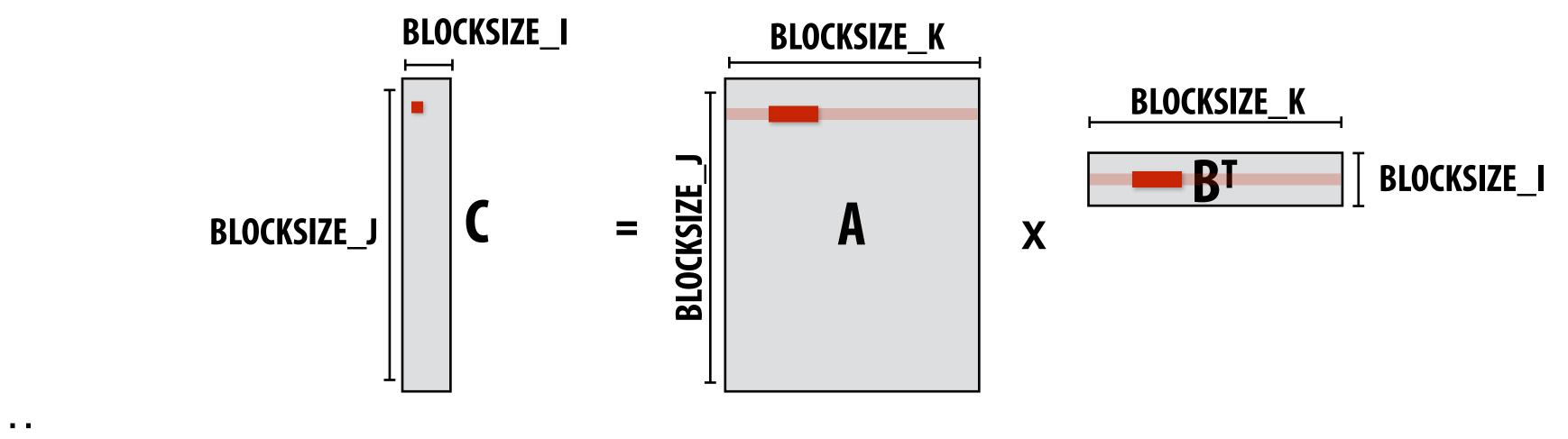


**Vectorize** i loop

Good: also improves spatial locality in access to B

Bad: working set increased by SIMD\_WIDTH, still walking over B in large steps

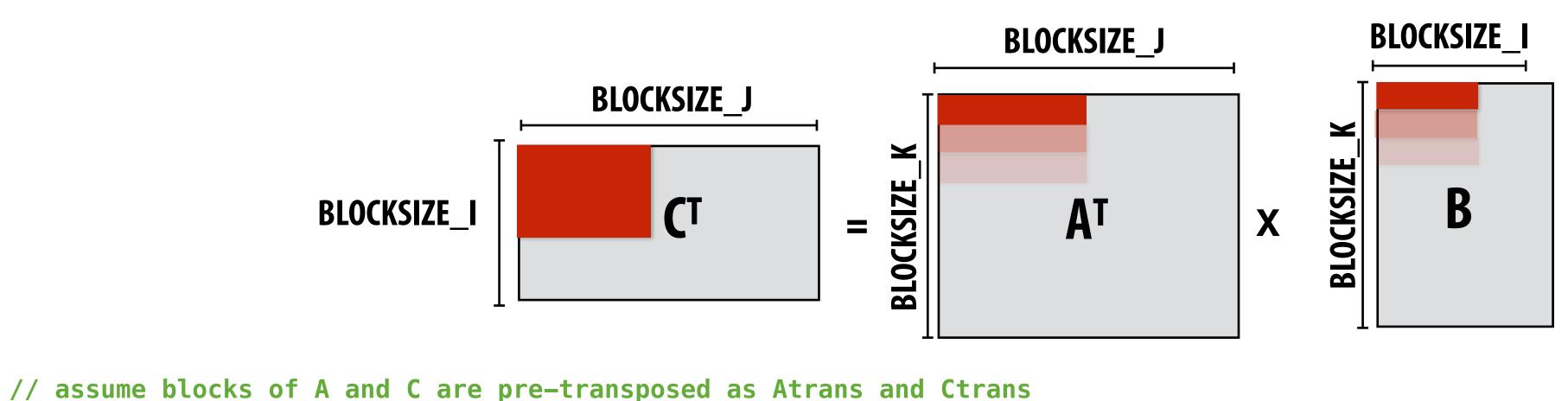
# Blocked dense matrix multiplication (2)



```
for (int j=0; j<BLOCKSIZE_J; j++)
  for (int i=0; i<BLOCKSIZE_I; i++) {
    float C_scalar = C[jblock+j][iblock+i];
    // C_scalar += dot(row of A,row of B)
    for (int k=0; k<BLOCKSIZE_K; k+=SIMD_WIDTH) {
        C_scalar += simd_dot(vec_load(&A[jblock+j][kblock+k]), vec_load(&Btrans[iblock+i][[kblock+k]);
    }
    C[jblock+j][iblock+i] = C_scalar;
}</pre>
```

Assume *i* dimension is small. Previous vectorization scheme (1) would not work well. Pre-transpose block of B (copy block of B to temp buffer in transposed form) Vectorize innermost loop

# Blocked dense matrix multiplication (3)

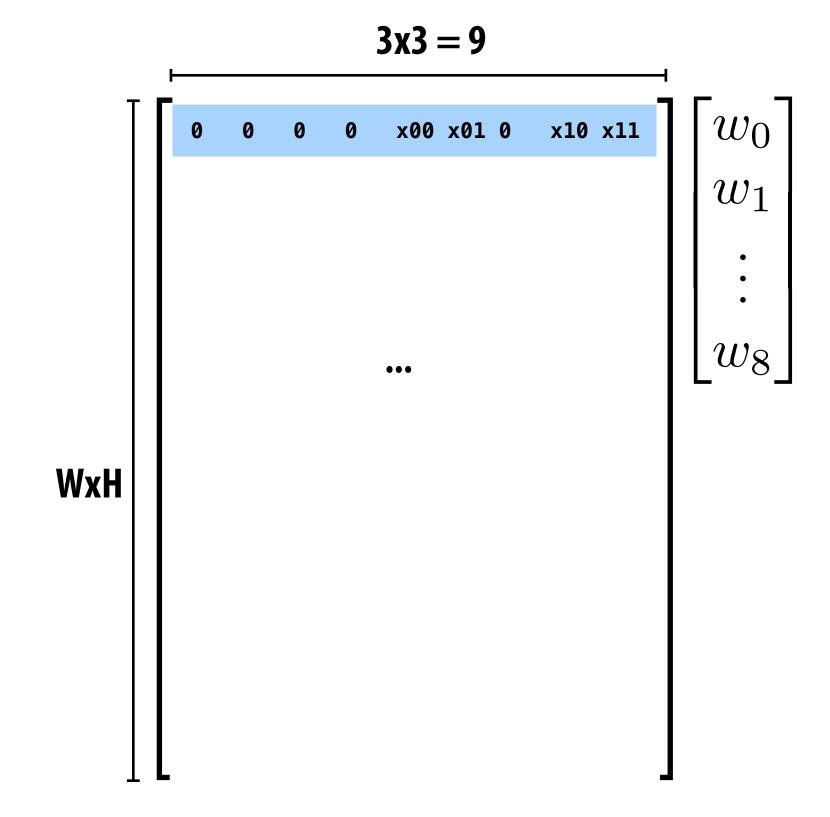


## Convolution as matrix-vector product

Construct matrix from elements of input image

_						ı	
	X <sub>00</sub>	X <sub>01</sub>	X <sub>02</sub>	X <sub>03</sub>	•••		
	X <sub>10</sub>	X <sub>11</sub>	X <sub>12</sub>	X <sub>13</sub>	•••		
Ī	<b>X</b> <sub>20</sub>	X <sub>21</sub>	X <sub>22</sub>	X <sub>23</sub>	•••		
	X <sub>30</sub>	<b>X</b> <sub>31</sub>	X <sub>32</sub>	<b>X</b> <sub>33</sub>	•••		
	•••	•••	•••	•••			

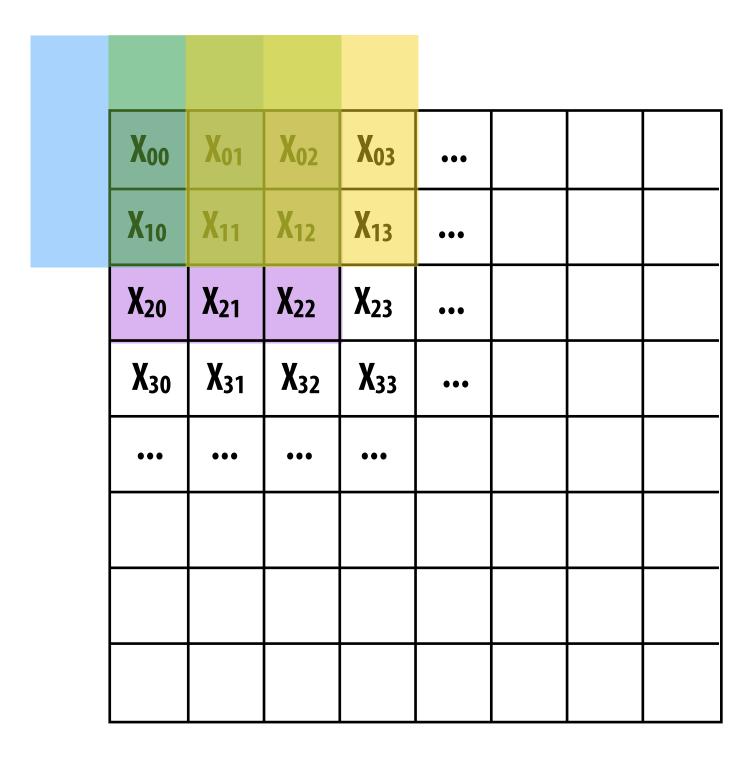
O(N) storage overhead for filter with N elements Must construct input data matrix



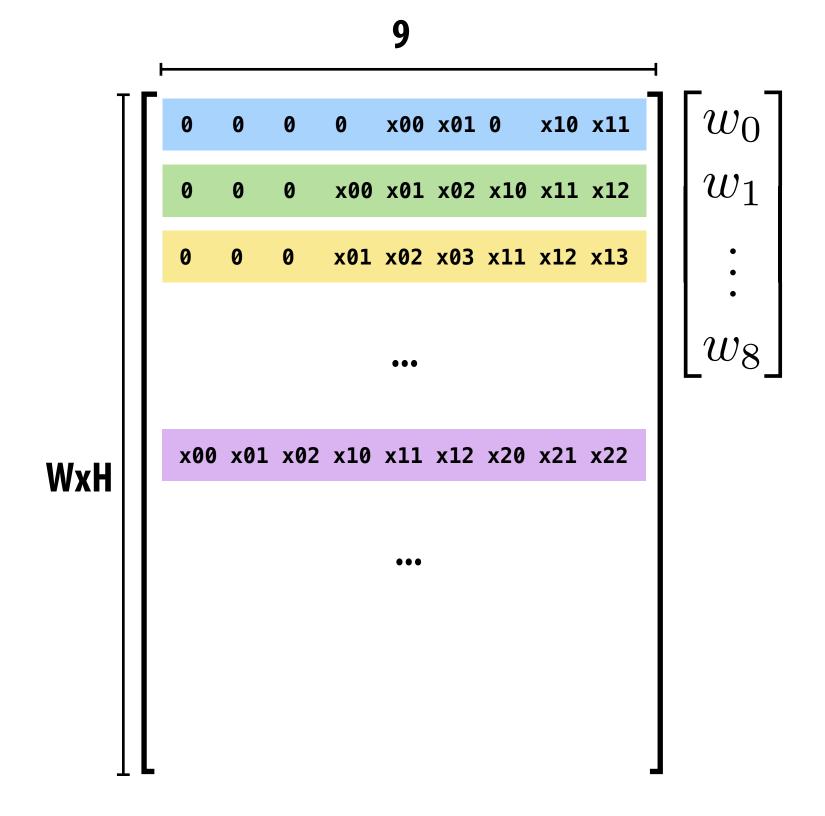
**Note: 0-pad matrix** 

## 3x3 convolution as matrix-vector product

Construct matrix from elements of input image

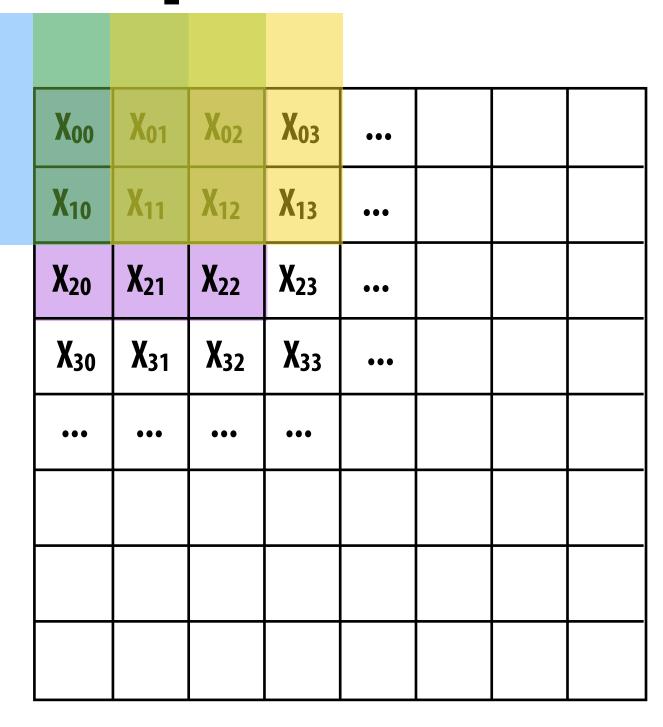


O(N) storage overhead for filter with N elements Must construct input data matrix



**Note: 0-pad matrix** 

## Multiple convolutions as matrix-matrix mult



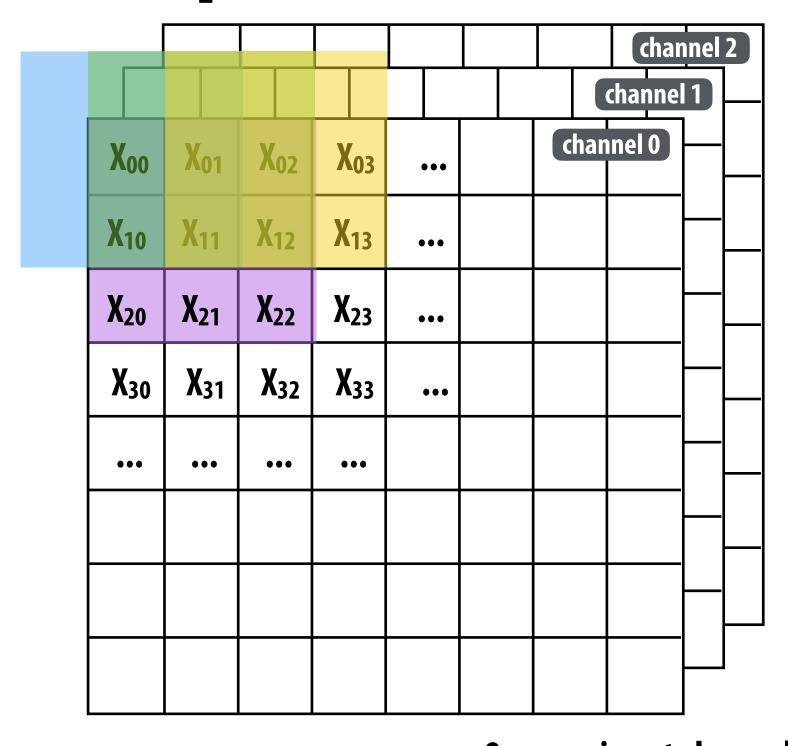
9 x00 x01 0 x10 x11 x00 x01 x02 x10 x11 x12 x01 x02 x03 x11 x12 x13 **WxH** 

x00 x01 x02 x10 x11 x12 x20 x21 x22

#### num filters

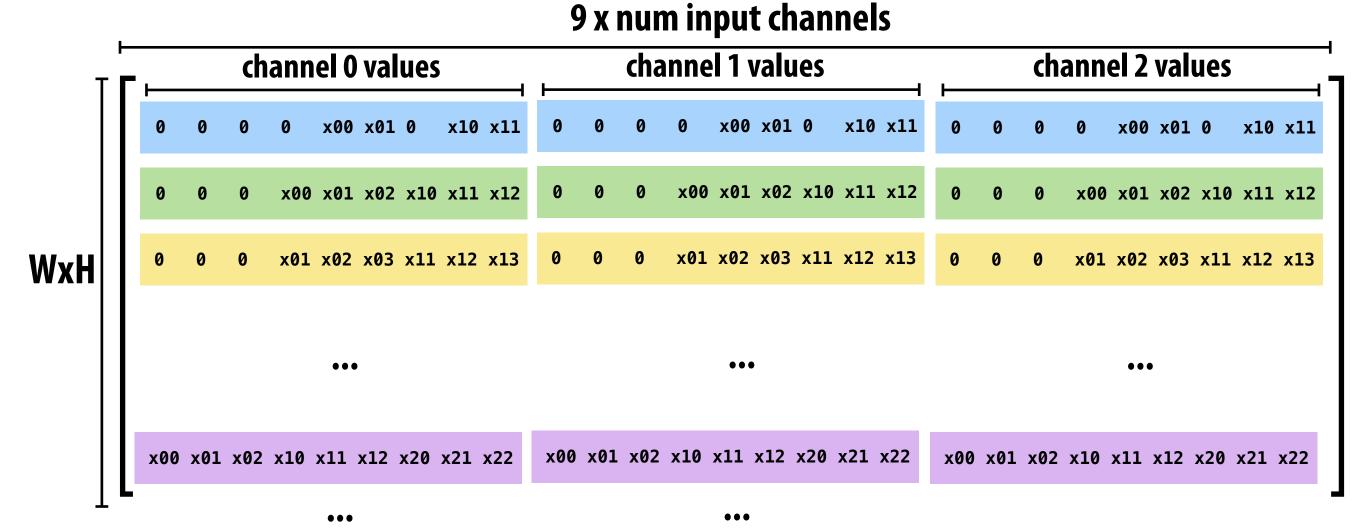
$\lceil w_{00} \rceil$	$w_{01}$	$w_{02}$	• • •	$w_{0N}$
$w_{10}$	$w_{11}$	$w_{12}$	• • •	$w_{0N}$
•	•	•		•
$\lfloor w_{80}  floor$	$w_{81}$	$w_{82}$	• • •	$w_{8N}$

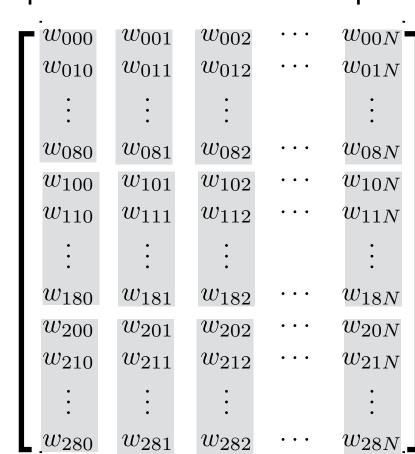
## Multiple convolutions on multiple input channels



For each filter, sum responses over input channels

Equivalent to (3 x 3 x num\_channels) convolution on (W x H x num\_channels) input data





num filters

Stanford CS149, Fall 2020

## Direct implementation of conv layer

```
float input[IMAGE_BATCH_SIZE][INPUT_HEIGHT][INPUT_WIDTH][INPUT_DEPTH];
float output[IMAGE_BATCH_SIZE][INPUT_HEIGHT][INPUT_WIDTH][LAYER_NUM_FILTERS];
float layer_weights[LAYER_NUM_FILTERS][LAYER_CONVY][LAYER_CONVX][INPUT_DEPTH];
// assumes convolution stride is 1
for (int img=0; img<IMAGE_BATCH_SIZE; img++)</pre>
   for (int j=0; j<INPUT_HEIGHT; j++)</pre>
      for (int i=0; i<INPUT_WIDTH; i++)</pre>
         for (int f=0; f<LAYER_NUM_FILTERS; f++) {</pre>
            output[img][j][i][f] = 0.f;
            for (int kk=0; kk<INPUT_DEPTH; kk++) // sum over filter responses of input channels
               for (int jj=0; jj<LAYER_FILTER_Y; jj++) // spatial convolution (Y)</pre>
                  for (int ii=0; ii<LAYER_FILTER_X; ii+) // spatial convolution (X)</pre>
                      output[img][j][i][f] += layer_weights[f][jj][ii][kk] * input[img][j+jj][i+ii][kk];
          }
```

Seven loops with significant input data reuse: reuse of filter weights (during convolution), and reuse of input values (across different filters)

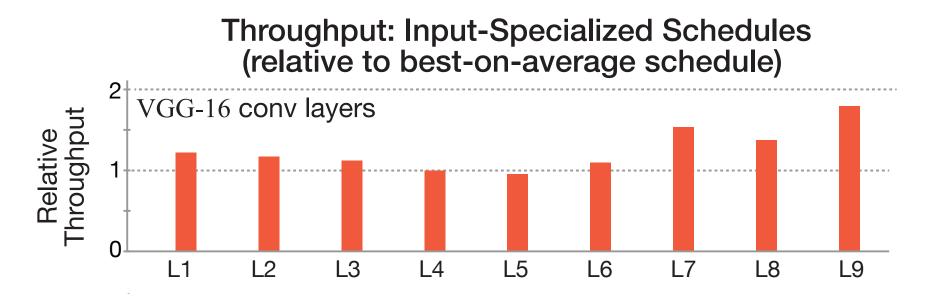
Avoids O(N) footprint increase by avoiding input matrix materialization But must roll your own highly optimized implementation of complicated loop nest.

## Convolutional layer in Halide

```
int in_w, in_h, in_ch = 4;
                                     // input params: assume initialized
Func in_func;
                                     // assume input function is initialized
int num_f, f_w, f_h, pad, stride; // parameters of the conv layer
Func forward = Func("conv");
                                     // n is minibatch dimension
Var x, y, z, n;
// This creates a padded input to avoid checking boundary
// conditions while computing the actual convolution
f_in_bound = BoundaryConditions::repeat_edge(in_func, 0, in_w, 0, in_h);
// Create buffers for layer parameters
Halide::Buffer<float> W(f_w, f_h, in_ch, num_f)
Halide::Buffer<float> b(num_f);
// domain of summation for filter with W x H x in_ch
RDom r(0, f_w, 0, f_h, 0, in_ch);
// Initialize to bias
forward(x, y, z, n) = b(z);
forward(x, y, z, n) += W(r.x, r.y, r.z, z) *
                       f_in_bound(x*stride + r.x - pad, y*stride + r.y - pad, r.z, n);
```

## Consider scheduling this seven-dimensional loop nest!

# Different layers of a single DNN may benefit from unique scheduling strategies

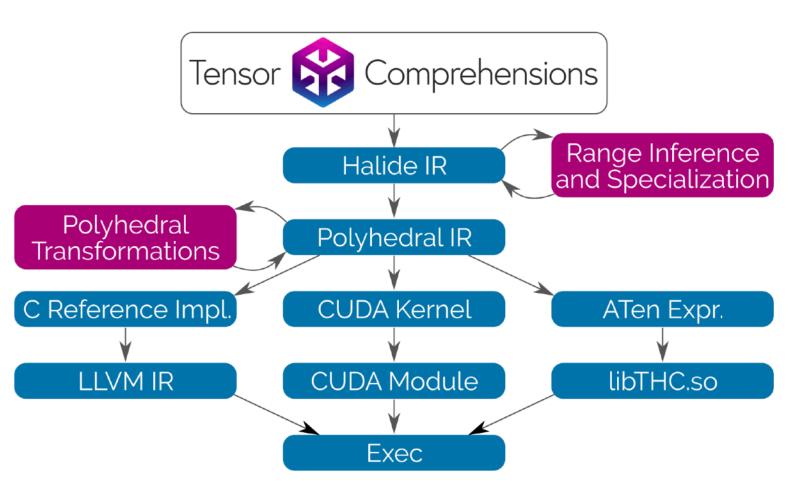


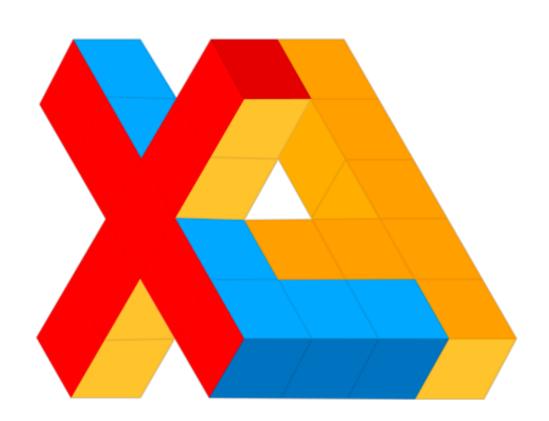
[Figure credit: Mullapudi et al. 2016]

Notice sizes of weights and activations in this network: (and consider SIMD widths of modern machines). Ug!

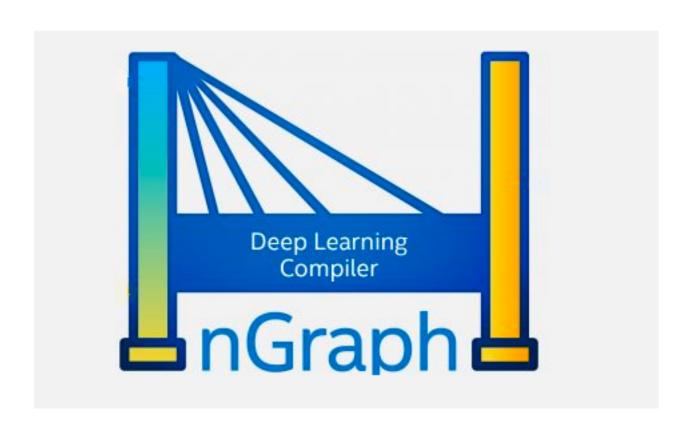
Tal <b>OptimizbilioneoBMarAualliy</b> eAuthored Schedules				
Type Astride	Filter Shape	Input Size		
Conv≠s2 LENSB	LBJR $3  imes 3  imes 32$	$224 \times 224 \times 3$		
Conv www s1	$3 \times 3 \times 32 \text{ dw}$	$112 \times 112 \times 32$		
Conv <del>ई</del> s1	$1 \times 1 \times 32 \times 64$	$112 \times 112 \times 32$		
Conv gw / s2	$3 \times 3 \times 64 \text{ dw}$	$112 \times 112 \times 64$		
Conv⊬sø	$1 \times 1 \times 64 \times 128$	$56 \times 56 \times 64$		
Conv dw / s1	$3 \times 3 \times 128$ dw	$56 \times 56 \times 128$		
Conv \( \frac{2}{5} \)1 \( \frac{1}{1} \) \( \frac{1}{1} \)	$1 \times 1 \times 128 \times 128$	$56 \times 56 \times 128$		
Converw / s2	$3 \times 3 \times 128 \text{ dw}$	$56 \times 56 \times 128$		
Conv Es1	$1 \times 1 \times 128 \times 256$	$28 \times 28 \times 128$		
Conv <del>g</del> w / s1	$3 \times 3 \times 256 \text{ dw}$	$28 \times 28 \times 256$		
Conv 2s1	$1 \times 1 \times 256 \times 256$	$28 \times 28 \times 256$		
Convidw/s2	$3 \times 3 \times 256 \mathrm{dw}$	$28 \times 28 \times 256$		
Conv / s1	$1 \times 1 \times 256 \times 512$	$14 \times 14 \times 256$		
5× Conv dw/ ME	$3 \times 512 \text{ dw}$	$14 \times 14 \times 512$		
Conv / sl	$1.1 \times 1 \times 512 \times 512$	$14 \times 14 \times 512$		
Conv tw 4 s2	$3 \times 3 \times 512 \text{ dw}$	$14 \times 14 \times 512$		
Conv 51	$1 \times 1 \times 512 \times 1024$	$7 \times 7 \times 512$		
Conv <b>©</b> w / s2	$3 \times 3 \times 1024 \text{ dw}$	$7 \times 7 \times 1024$		
Conv ∉s l <sub>0</sub>	$1 \times 01 \times 1024 \times 20024$	$7 \times 70 \times 1024$ 40		
Avg Pool / s1	Pool Søhødule develop	m7ent finnel(002n4utes)		
FC / s1 = Pro	gilalizaher 11000 $\blacksquare$ = Prog	grān $m$ e $\approx$ 2 $1024$ = Auto-s		
Softmax / s1	Classifier	$1 \times 1 \times 1000$		

# Many efforts to automatically schedule key DNN operations





## StVM Open Deep Learning Compiler Stack



Documentation | Contributors | Community | Release Notes

TVM is a compiler stack for deep learning systems. It is designed to close the gap between the productivity-focused deep learning frameworks, and the performance- and efficiency-focused hardware backends. TVM works with deep learning frameworks to provide end to end compilation to different backends. Checkout the tvm stack homepage for more information.

#### **NVIDIA TensorRT**

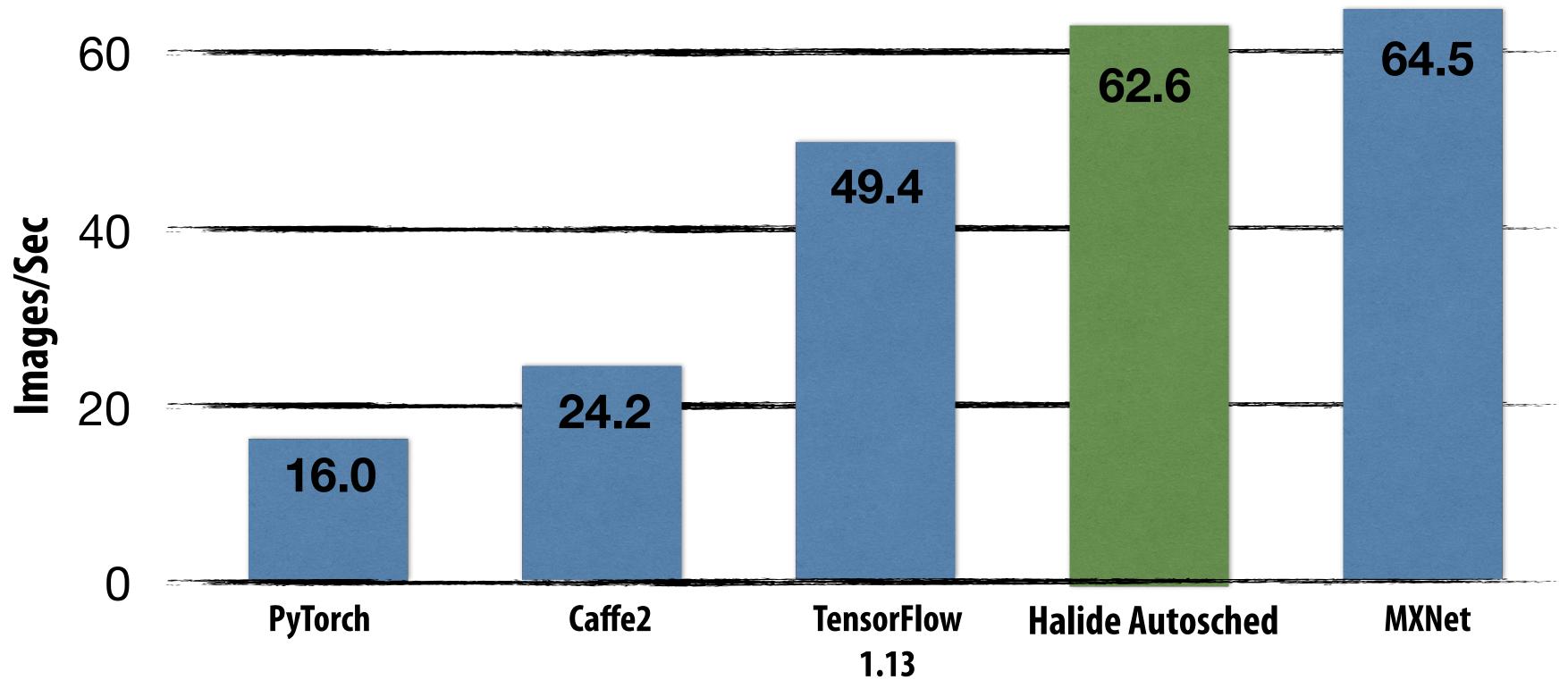
license Apache 2.0 build passing

Programmable Inference Accelerator

# Halide autoscheduler produces efficient DNN layer implementations (for CPUs)

Use large database of programs to learn to predict performance of Halide program+schedule. Then search for best performing programs.





# Reminder: energy cost of data access

Significant fraction of energy expended moving data to processor ALUs

Operation	Energy [pJ]	Relative Cost
32 bit int ADD	0.1	1
32 bit float ADD	0.9	9
32 bit Register File	1	10
32 bit int MULT	3.1	31
32 bit float MULT	3.7	37
32 bit SRAM Cache	5	50
32 bit DRAM Memory	640	6400

**Estimates for 45nm process** 

[Source: Mark Horowitz]

1

## Reducing network footprint

- Early DNN designs: large storage cost for model parameters
  - AlexNet model: ~200 MB
  - VGG-16 model: ~500 MB
  - ResNet-50: 102 MB
  - Inception-v3: 91 MB

- In modern DNNs, activations (intra-layer intermediate buffers) require much more storage than weights
  - Consider  $28 \times 28 \times 256$  channels x batch size 64 = 52 MB
  - So bandwidth is often due to reading/writing intermediate values to memory

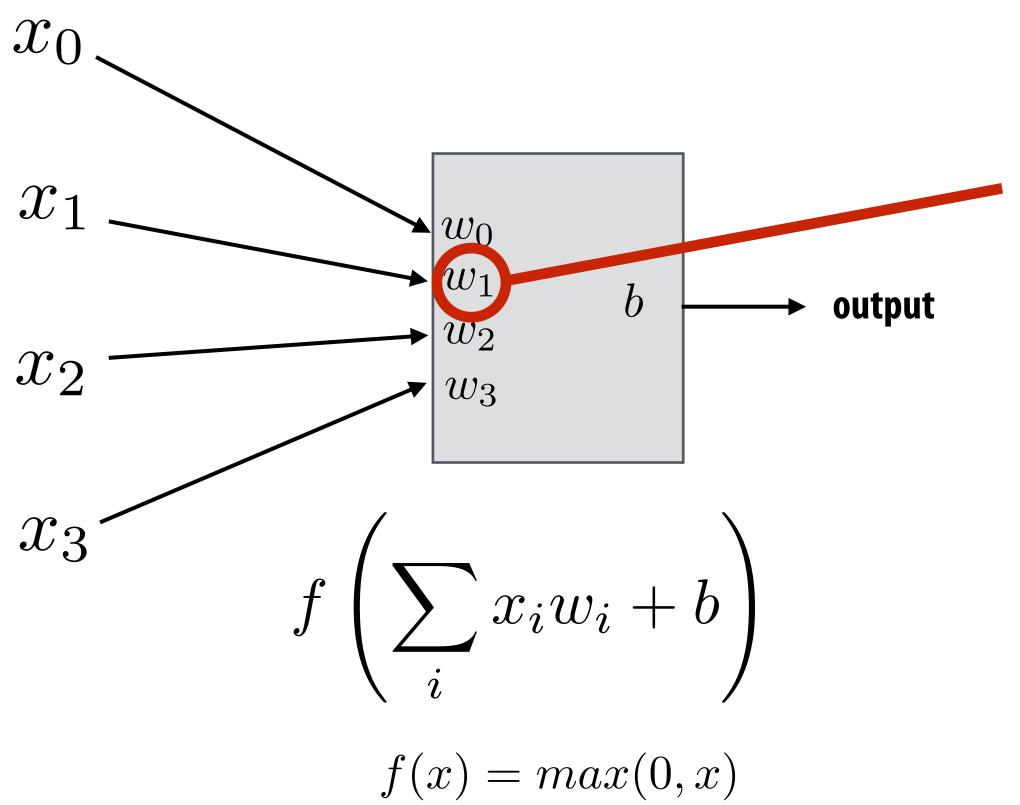






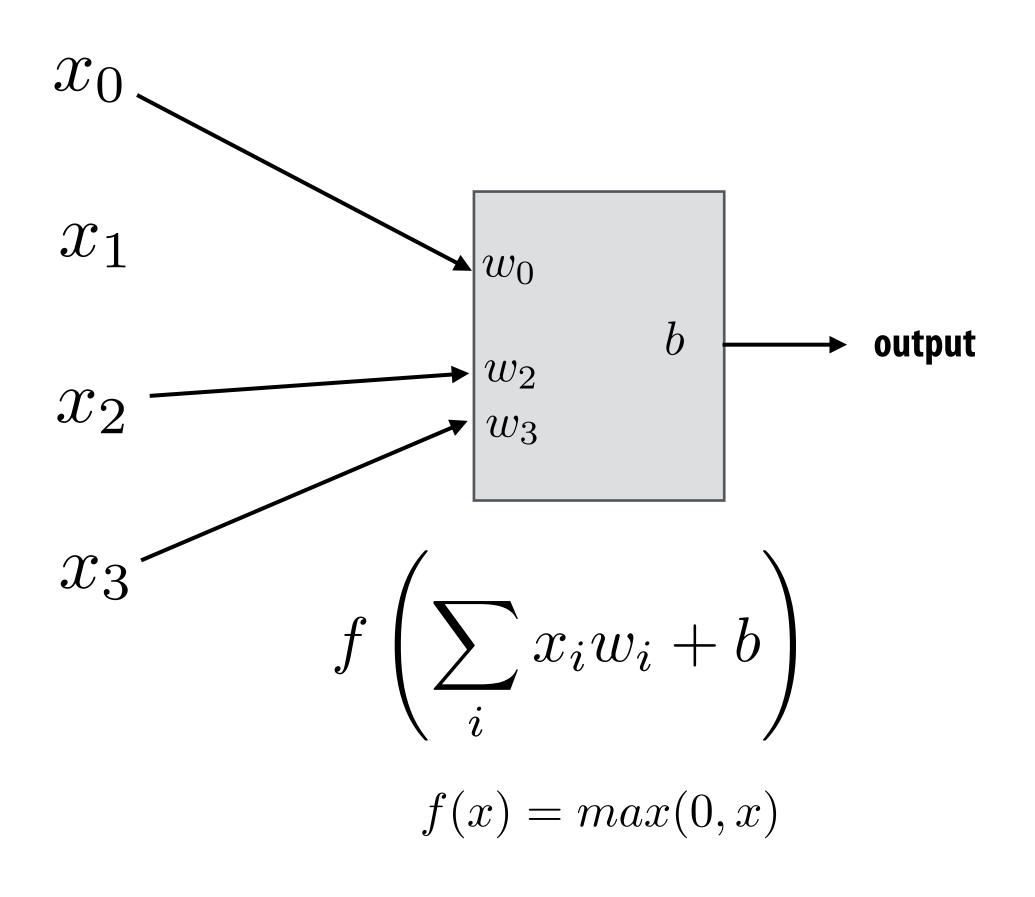
# Is there an opportunity for compression?

## "Pruning" (sparsifying) a network



If weight is near zero, then corresponding input has little impact on output of neuron.

## "Pruning" (sparsifying) a network



Idea: prune connections with near zero weight

Remove entire units if all connections are pruned.

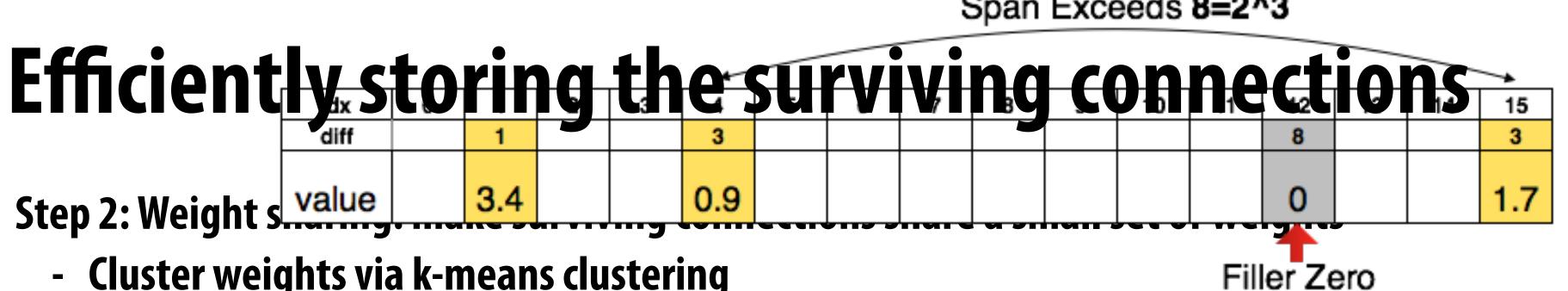
## Representing "sparsified" networks

Step 1: prune low-weight links (iteratively retrain network, then prune)

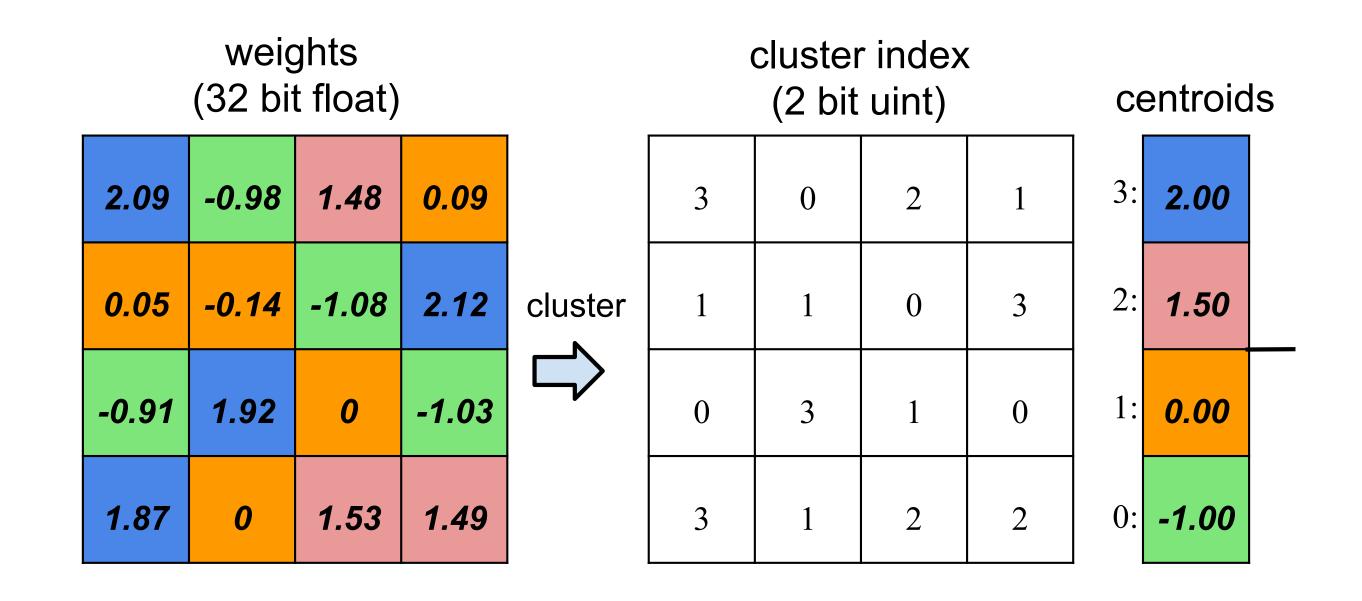
- Store weight matrices in compressed sparse row (CSR) format

Reduce storage over head of indices by delta encoding them to fit in 8 bits

```
Indices 1 3 5 ... Value 1.8 0.5 2.1
```



- Cluster weights via k-means clustering
- Compress weights by only storing index of assigned cluster (lg(k) bits)
- This is a form of lossy compression



Step 3: Huffman encode quantized weights and CSR indices (lossless compression)

## VGG-16 sparsification

Large savings in fully connected layers due to combination of pruning, quantization, Huffman encoding \*

Layer	#Weights	Weights% (P)	Weigh bits (P+Q)	Weight bits (P+Q+H)	Index bits (P+Q)	Index bits (P+Q+H)	Compress rate (P+Q)	Compress rate (P+Q+H)
conv1_1	2K	58%	8	6.8	5	1.7	40.0%	29.97%
$conv1_2$	37K	22%	8	6.5	5	2.6	9.8%	6.99%
$conv2_{-}1$	74K	34%	8	5.6	5	2.4	14.3%	8.91%
$conv2_2$	148K	36%	8	5.9	5	2.3	14.7%	9.31%
conv3_1	295K	53%	8	4.8	5	1.8	21.7%	11.15%
$conv3_2$	590K	24%	8	4.6	5	2.9	9.7%	5.67%
conv3_3	590K	42%	8	4.6	5	2.2	17.0%	8.96%
$conv4_1$	1 <b>M</b>	32%	8	4.6	5	2.6	13.1%	7.29%
$conv4_2$	2M	27%	8	4.2	5	2.9	10.9%	5.93%
conv4_3	2M	34%	8	4.4	5	2.5	14.0%	7.47%
$conv5_1$	2M	35%	8	4.7	5	2.5	14.3%	8.00%
$conv5_2$	2M	29%	8	4.6	5	2.7	11.7%	6.52%
$conv5_3$	2M	36%	8	4.6	5	2.3	14.8%	7.79%
fc6	103M	4%	5	3.6	5	3.5	1.6%	1.10%
fc7	17M	4%	5	4	5	4.3	1.5%	1.25%
fc8	4M	23%	5	4	5	3.4	7.1%	5.24%
Total	138M	$7.5\%(13\times)$	6.4	4.1	5	3.1	3.2% ( <b>31</b> ×)	2.05% ( <b>49</b> ×)

**P** = connection pruning (prune low weight connections)

**Q** = quantize surviving weights (using shared weights)

H = Huffman encode

#### **ImageNet Image Classification Performance**

	Top-1 Error	Top-5 Error	<b>Model size</b>	
VGG-16 Ref	31.50%	11.32%	552 MB	
VGG-16 Compressed	31.17%	10.91%	11.3 MB	$oldsymbol{49} imes$

<sup>\*</sup> Benefits of automatic pruning apply mainly to fully connected layers, but unfortunately many modern networks are dominated by costs of convolutional layers

## Compressing weights (and activations)

- Many efforts to use low precision values for DNN weights and intermediate activations
- In the extreme case: 1-bit

#### XNOR-Net: ImageNet Classification Using Binary Convolutional Neural Networks

Mohammad Rastegari<sup>†</sup>, Vicente Ordonez<sup>†</sup>, Joseph Redmon\*, Ali Farhadi<sup>†</sup>\*

Allen Institute for AI<sup>†</sup>, University of Washington\* {mohammadr, vicenteor}@allenai.org {pjreddie, ali}@cs.washington.edu

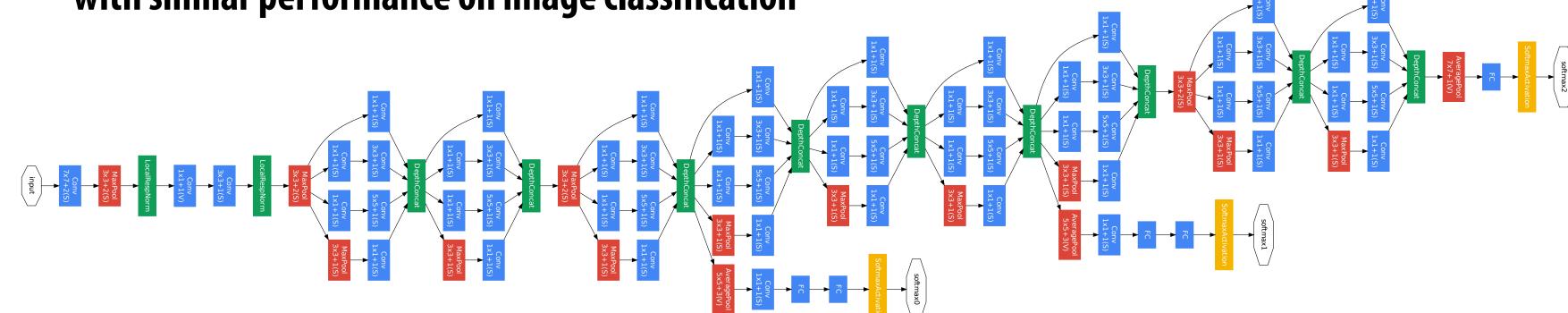
Abstract. We propose two efficient approximations to standard convolutional neural networks: Binary-Weight-Networks and XNOR-Networks. In Binary-Weight-Networks, the filters are approximated with binary values resulting in 32× memory saving. In XNOR-Networks, both the filters and the input to convolutional layers are binary. XNOR-Networks approximate convolutions using primarily binary operations. This results in 58× faster convolutional operations (in terms of number of the high precision operations) and 32× memory savings. XNOR-Nets offer the possibility of running state-of-the-art networks on CPUs (rather than GPUs) in real-time. Our binary networks are simple, accurate, efficient, and work on challenging visual tasks. We evaluate our approach on the ImageNet classification task. The classification accuracy with a Binary-Weight-Network version of AlexNet is the same as the full-precision AlexNet. We compare our method with recent network binarization methods, BinaryConnect and BinaryNets, and outperform these methods by large margins on ImageNet, more than 16% in top-1 accuracy. Our code is available at: http://allenai.org/plato/xnornet.

# This a great example of non-domain-specific vs. domain-specific approach to innovation

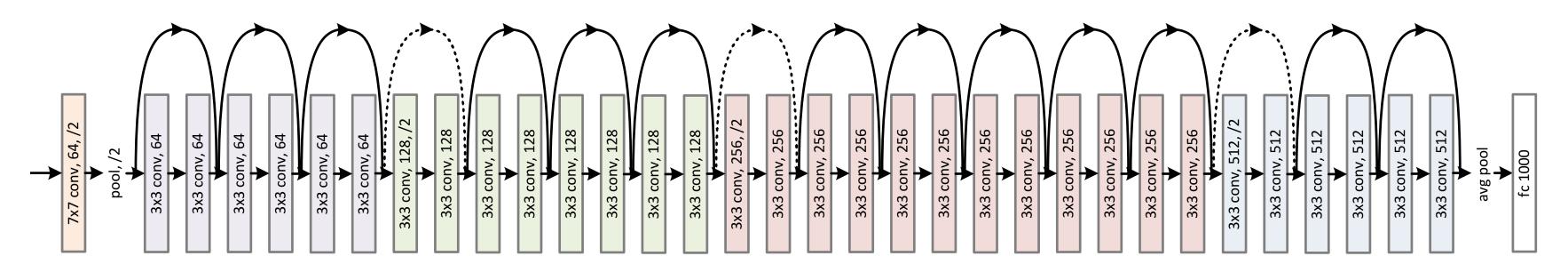
# Leveraging domain-knowledge: more efficient topologies (aka better algorithm design)

- Original DNNs for image recognition where over-provisioned
  - Large filters, many filters
- Modern DNNs designs are hand-designed to be sparser

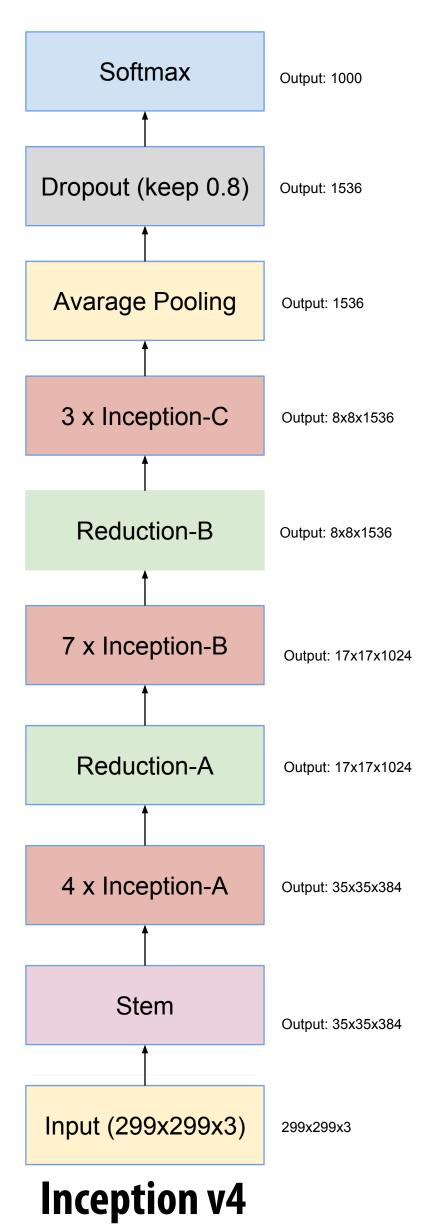
SqueezeNet: [landola 2017] Reduced number of parameters in AlexNet by 50x, with similar performance on image classification

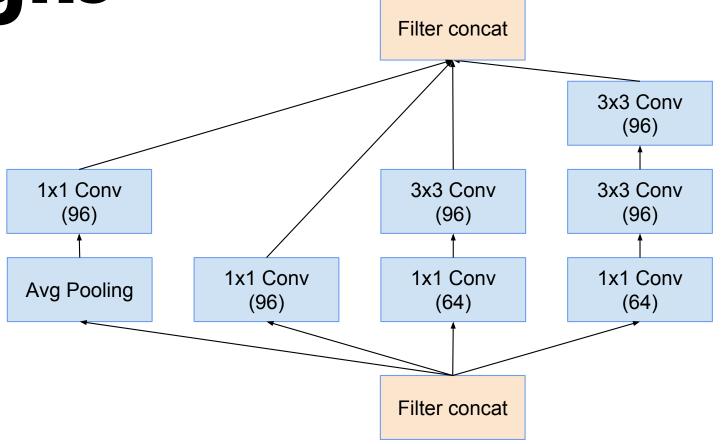


Inception v1 (GoogleLeNet) — 27 total layers, 7M parameters

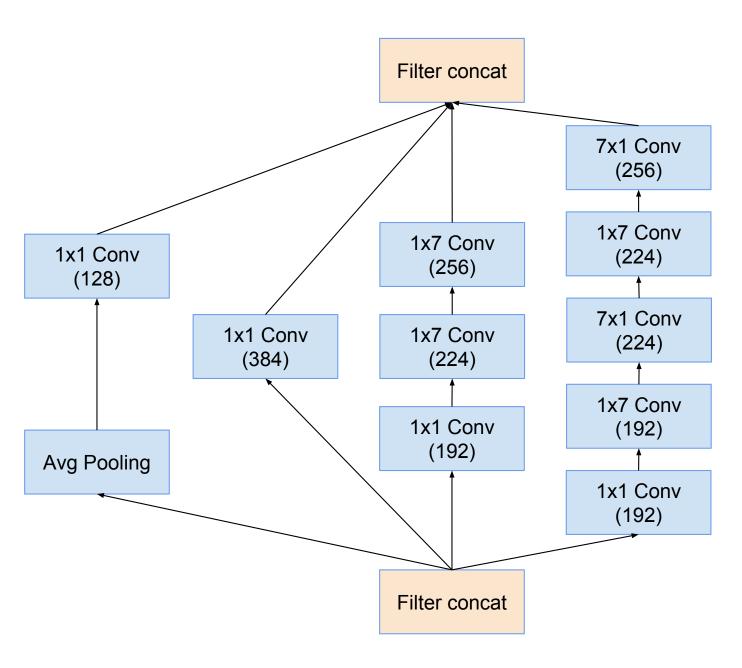


Modular network designs



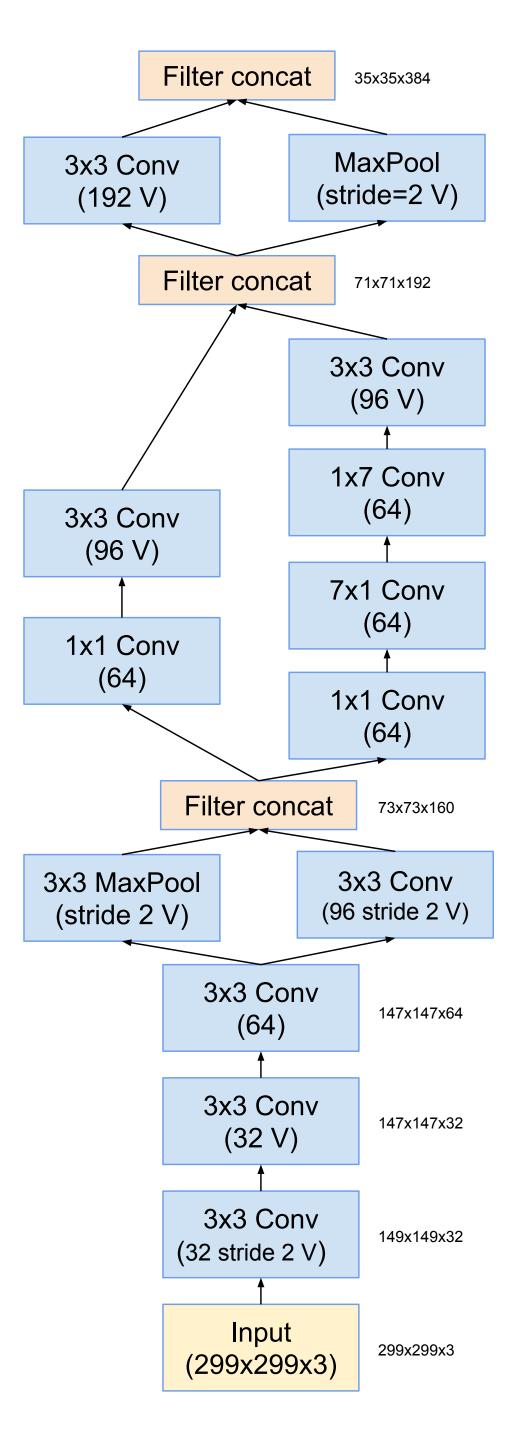


A block

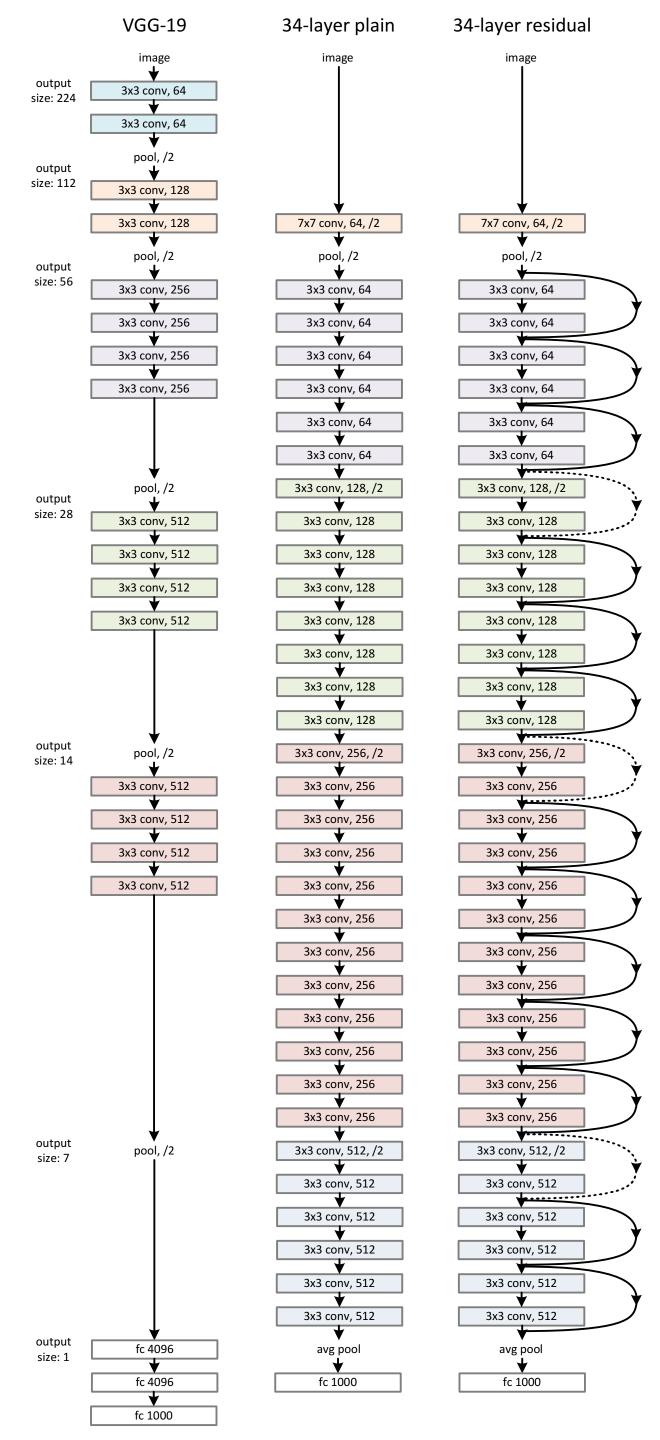


**B** block

## Inception stem



## ResNet



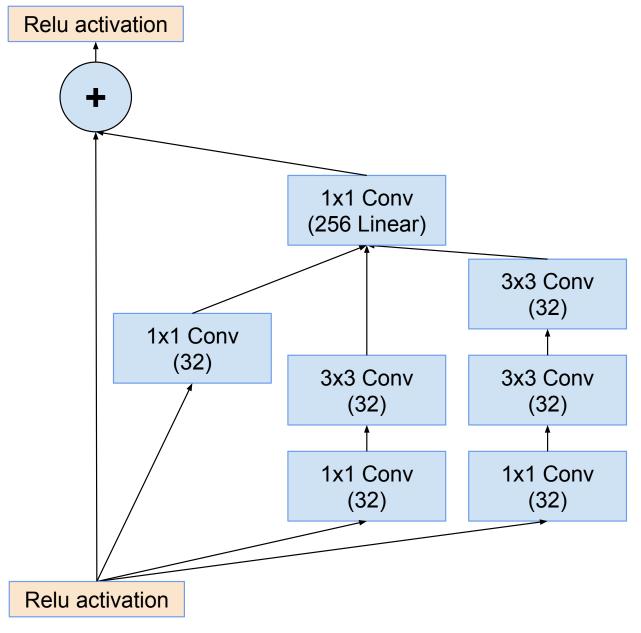
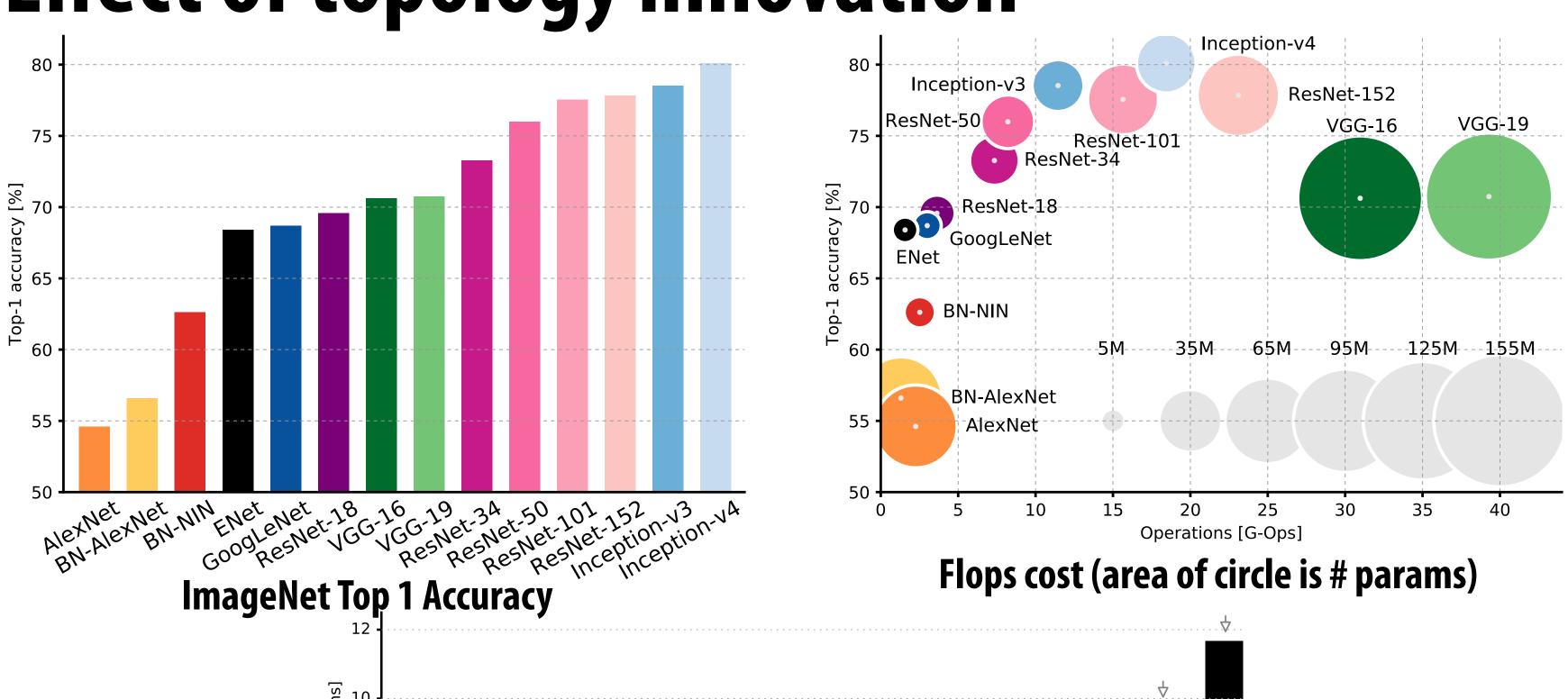
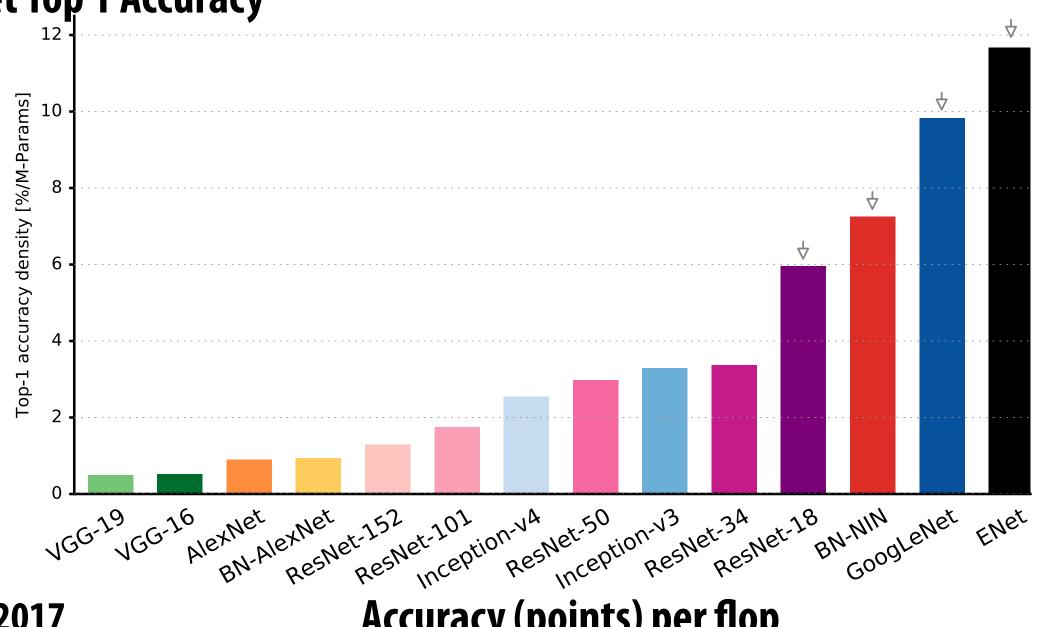


Figure 10. The schema for  $35 \times 35$  grid (Inception-ResNet-A) module of Inception-ResNet-v1 network.

## Effect of topology innovation





**Accuracy (points) per flop** 

## Improving accuracy/cost (image classification)

2014 → 2017 ~ 25x improvement in cost at similar accuracy

	<b>ImageNet Top-1</b>		Cost/image	
	Accuracy	<b>Num Params</b>	(MADDs)	
VGG-16	71.5%	138M	15B	[2014]
GoogleNet	<b>70</b> %	6.8M	1.5B	[2015]
ResNet-18	<b>73%</b> *	11.7M	1.8B	[2016]
<b>MobileNet-224</b>	<b>70.5</b> %	4.2M	0.6B	[2017]

<sup>\* 10-</sup>crop results (ResNet 1-crop results are similar to other DNNs in this table)

## MobileNet

#### [Howard et al. 2017]

### 3x3 Conv BN

3x3 Depthwise Conv BN ReLU

1x1 Conv

BN

ReLU

# ReLU

#### Table 1. MobileNet Body Architecture

Factor NUM\_FILTERS 3x3xNUM\_CHANNELS convolutions into:

NUM\_CHANNELS 3x3x1 convolutions for each input channel

And NUM\_FILTERS 1x1xNUM\_CHANNELS convolutions to combine the results

Type / Stride	Filter Shape	Input Size					
Conv / s2	$3 \times 3 \times 3 \times 32$	$224 \times 224 \times 3$					
Conv dw / s1	$3 \times 3 \times 32 \text{ dw}$	$112 \times 112 \times 32$					
Conv / s1	$1 \times 1 \times 32 \times 64$	$112 \times 112 \times 32$					
Conv dw / s2	$3 \times 3 \times 64 \text{ dw}$	$\boxed{112 \times 112 \times 64}$					
Conv / s1	$1 \times 1 \times 64 \times 128$	$\boxed{56 \times 56 \times 64}$					
Conv dw / s1	$3 \times 3 \times 128 \text{ dw}$	$56 \times 56 \times 128$					
Conv / s1	$1 \times 1 \times 128 \times 128$	$56 \times 56 \times 128$					
Conv dw / s2	$3 \times 3 \times 128 \text{ dw}$	$56 \times 56 \times 128$					
Conv / s1	$1 \times 1 \times 128 \times 256$	$28 \times 28 \times 128$					
Conv dw / s1	$3 \times 3 \times 256 \text{ dw}$	$28 \times 28 \times 256$					
Conv / s1	$1 \times 1 \times 256 \times 256$	$28 \times 28 \times 256$					
Conv dw / s2	$3 \times 3 \times 256 \text{ dw}$	$28 \times 28 \times 256$					
Conv / s1	$1 \times 1 \times 256 \times 512$	$14 \times 14 \times 256$					
$5 \times \text{Conv dw / s1}$	$3 \times 3 \times 512 \text{ dw}$	$\boxed{14 \times 14 \times 512}$					
Conv / s1	$1 \times 1 \times 512 \times 512$	$14 \times 14 \times 512$					
Conv dw / s2	$3 \times 3 \times 512 \text{ dw}$	$14 \times 14 \times 512$					
Conv / s1	$1 \times 1 \times 512 \times 1024$	$7 \times 7 \times 512$					
Conv dw / s2	$3 \times 3 \times 1024 \text{ dw}$	$7 \times 7 \times 1024$					
Conv / s1	$1 \times 1 \times 1024 \times 1024$	$7 \times 7 \times 1024$					
Avg Pool / s1	Pool $7 \times 7$	$7 \times 7 \times 1024$					
FC / s1	$1024 \times 1000$	$1 \times 1 \times 1024$					
Softmax / s1	Classifier	$1 \times 1 \times 1000$					

#### Image classification (ImageNet) **Comparison to Common DNNs**

Model	ImageNet	Million	Million
	Accuracy	Mult-Adds	Parameters
1.0 MobileNet-224	70.6%	569	4.2
GoogleNet	69.8%	1550	6.8
VGG 16	71.5%	15300	138

#### Image classification (ImageNet) **Comparison to Other Compressed DNNs**

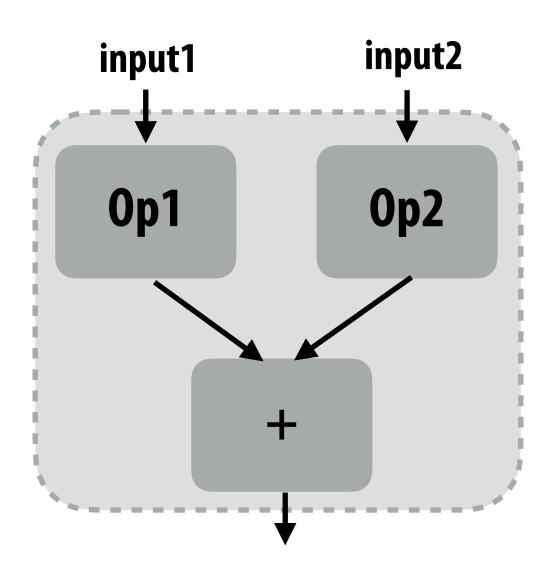
Model	ImageNet	Million	Million
	Accuracy	Mult-Adds	Parameters
0.50 MobileNet-160	60.2%	76	1.32
Squeezenet	57.5%	1700	1.25
AlexNet	57.2%	720	60

## Model optimization techniques

- Manually designing better models
  - Common parameters: depth of network, width of filters, number of filters per layer, convolutional stride, etc.
- Good scheduling of performance-critical operations (layers)
  - Loop blocking/tiling, fusion
  - Typically optimized manually by humans (but significant research efforts to automate scheduling)
- Compressing models
  - Lower bit precision
  - Automatic sparsification/pruning
- Automatically discovering efficient model topologies (architecture search)

### DNN architecture search

- Learn an efficient DNN topology along with associated weights
- Example: progressive neural architecture search [Liu et al. 18]



#### **Eight possible operations:**

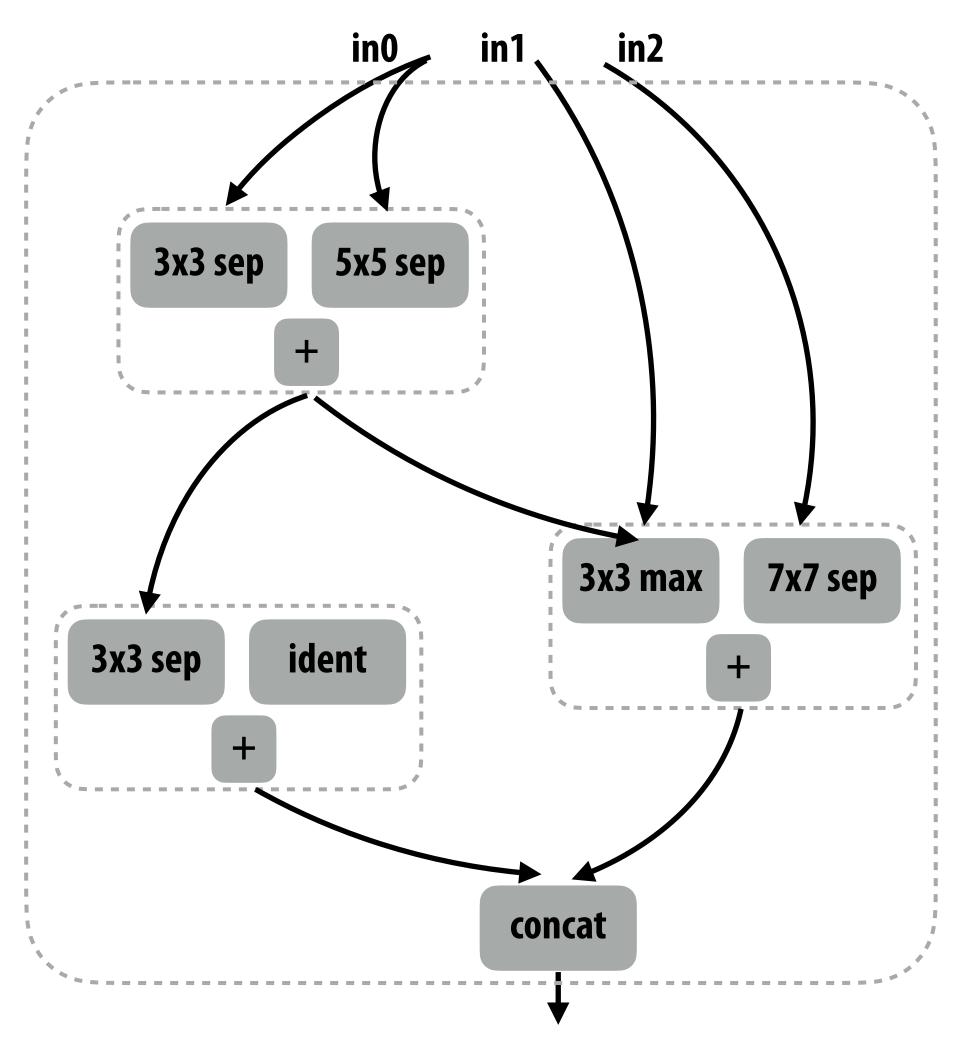
3x3 depthwise-separable conv 5x5 depthwise-separable conv 7x7 depthwise-separable conv 1x7 followed by 7x1 conv

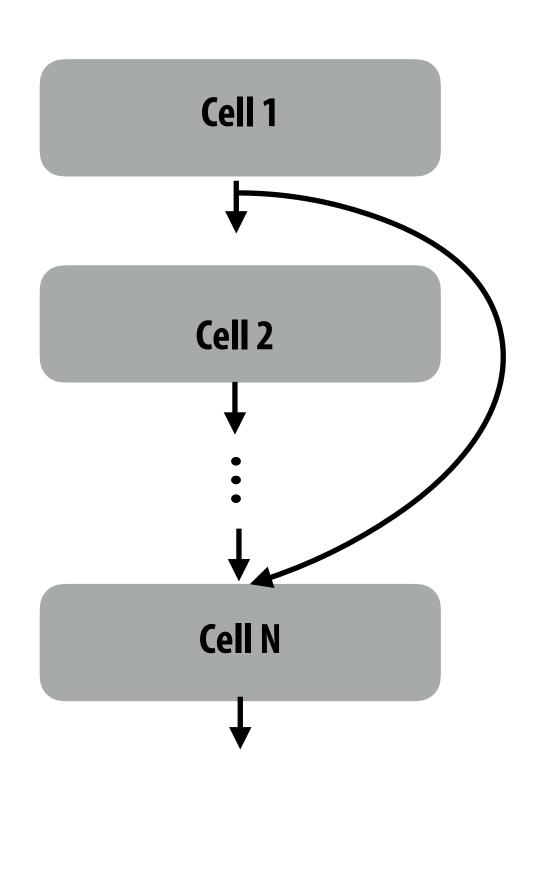
identity3x3 average pool3x3 max pool3x3 dilated conv

## Architecture search space

Cells are DAGs of B blocks

#### DNNs are sequences of N cells





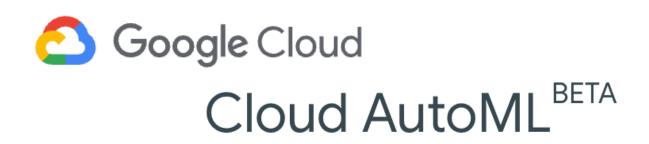
Cells have one output, can receive input from all prior cells

## Progressive neural architecture search results

 Automatic search was able to find model architectures that yielded similar/ better accuracy to hand designed models (and comparable costs)

Model	Params	Mult-Adds	Top-1	Top-5
MobileNet-224 [14]	4.2M	569M	70.6	89.5
ShuffleNet (2x) [37]	5M	524M	70.9	89.8
NASNet-A $(N = 4, F = 44)$ [41]	5.3M	564M	74.0	91.6
AmoebaNet-B $(N = 3, F = 62)$ [27]	5.3M	555M	74.0	91.5
AmoebaNet-A $(N = 4, F = 50)$ [27]	5.1M	555M	74.5	92.0
AmoebaNet-C $(N = 4, F = 50)$ [27]	6.4M	570M	75.7	92.4
PNASNet-5 $(N = 3, F = 54)$	5.1M	588M	74.2	91.9

 Forms of architecture search implemented by Cloud-based ML hosting services (user provides training data, service searches for good model)





# Why might a GPU be a good platform for DNN evaluation?

consider: arithmetic intensity, SIMD, dataparallelism, memory bandwidth requirements

## Deep neural networks on GPUs

- Many high-performance DNN implementations target GPUs
  - High arithmetic intensity computations (computational characteristics similar to dense matrix-matrix multiplication)
  - Benefit from flop-rich architectures
  - Highly-optimized library of kernels exist for GPUs (cuDNN)

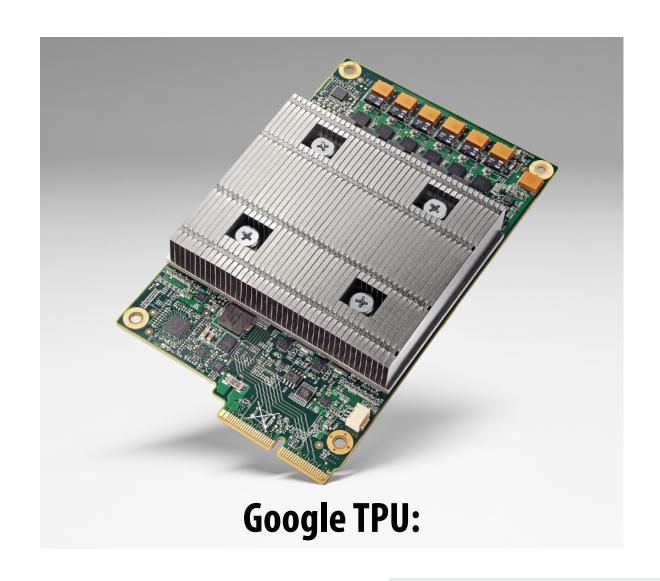


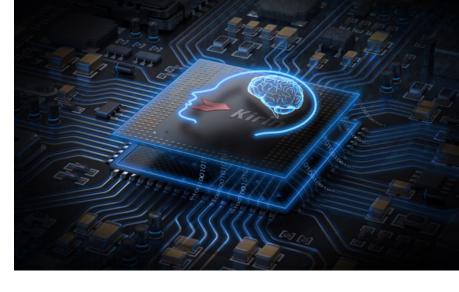
# Why might a GPU be a sub-optimal platform for DNN evaluation?

consider: is a general purpose processor needed?

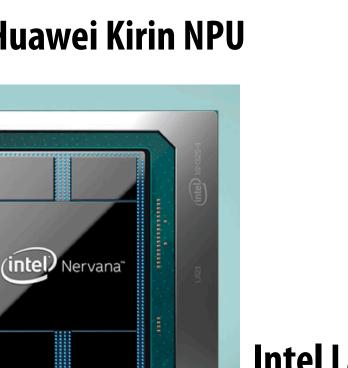
### Hardware acceleration for DNNs

SambaNova® S Y S T E M S



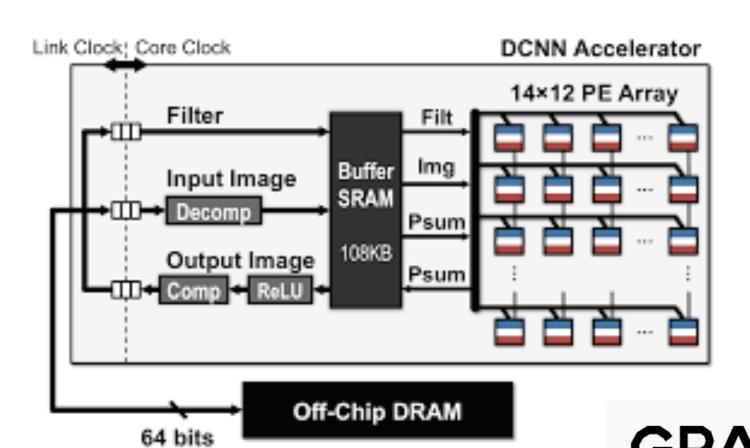


**Huawei Kirin NPU** 





**Apple Neural Engine** 



**MIT Eyeriss** 

GRAPHCORE

**Intel Lake Crest Deep Learning Accelerator** 



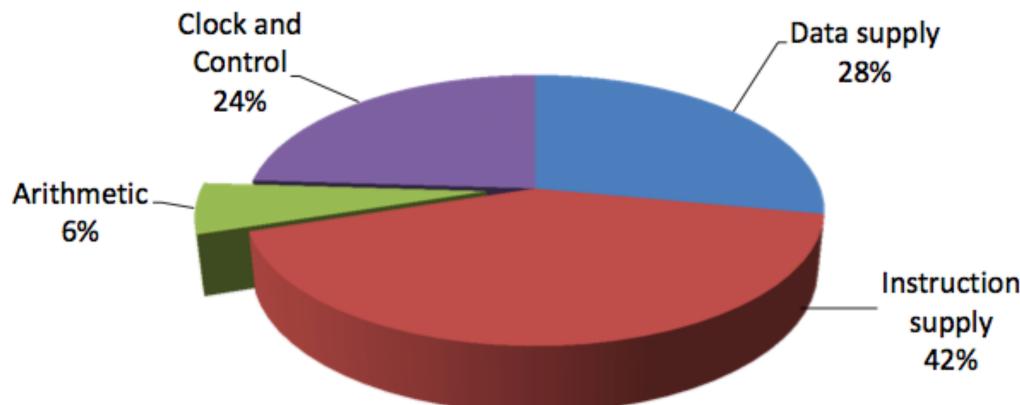
Slide credit: Xuan Yang

## Recall: properties of GPUs

- "Compute rich": packed densely with processing elements
  - Good for compute-bound applications
- Good, because dense-matrix multiplication and DNN convolutional layers (when implemented properly) are compute bound

But recall cost of instruction stream processing and control in a programmable processor:

Note: these figures are estimates for a CPU:



Efficient Embedded Computing [Dally et al. 08]
[Figure credit Eric Chung]

## One solution: more complex instructions

- Fused multiply add (ax + b)
- 4-component dot product x = A dot B
- 4x4 matrix multiply
  - AB + C for 4x4 matrices A, B, C

 Key principle: amortize cost of instruction stream processing across many operations of a single complex instruction

## Volta GPU



Each SM core has: 64 fp32 ALUs (mul-add) 32 fp64 ALUs

8 "tensor cores"

Execute 4x4 matrix mul-add instr

A x B + C for 4x4 matrices A,B,C

A, B stored as fp16, accumulation with fp32 C

There are 80 SM cores in the GV100 GPU: 5,120 fp32 mul-add ALUs

640 tensor cores

6 MB of L2 cache

1.5 GHz max clock

= 15.7 TFLOPs fp32

= 125 TFLOPs (fp16/32 mixed) in tensor cores

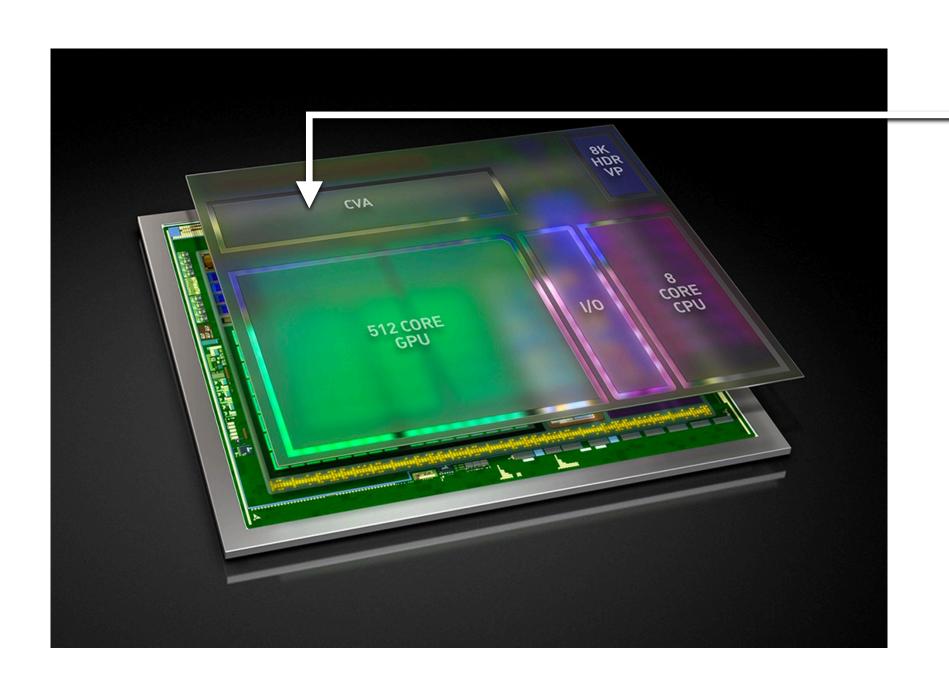
# Efficiency estimates \*

Estimated overhead of programmability (instruction stream, control, etc.)

- Half-precision FMA (fused multiply-add) 2000%

- Half-precision DP4 (vec4 dot product) 500%

- Half-precision MMA (matrix-matrix multiply + accumulate) 27%



**NVIDIA Xavier (SoC for automotive domain)** 

Features a Computer Vision Accelerator (CVA), a custom module for deep learning acceleration (large matrix multiply unit)

But only 2x more efficient than Volta MMA instruction despite being highly specialized component. (includes optimization of gating multipliers if either operand is zero)

<sup>\*</sup> Estimates by Bill Dally using academic numbers, SysML talk, Feb 2018

# Summary: efficiently evaluating deep nets

- Workload characteristics for image processing DNNs:
  - Convlayers: high arithmetic intensity, significant portion of cost when evaluating DNNs for computer vision
- Significant interest in reducing size of DNNs for more efficiency evaluation
- Algorithmic techniques (better DNN model architectures) are responsible for significant speedups in recent years
  - Expect increasing use of automated model search techniques
- Huge innovation in specialized hardware accelerators